

# Freeze-in Production of Non-Abelian Millicharged Vector Dark Matter

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Based on [arXiv: 2512.08622](#), [2408.11626](#), [2605.03427](#), [2111.15503](#)

In collaboration with C.R.Chen (NTNU), M. Du, R. Fang, Z. Liu (NJU), T.C. Yuan (AS)

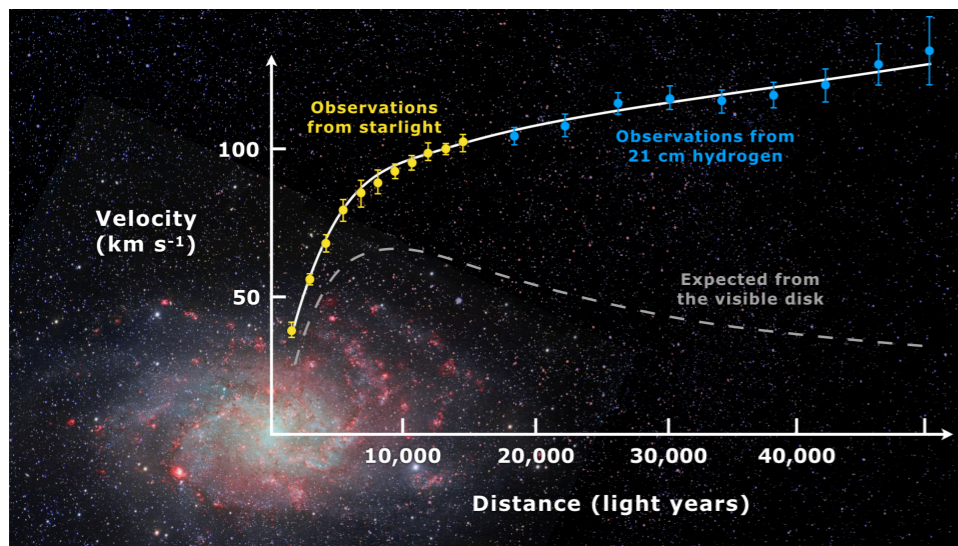
The 16th Particle Physics Phenomenology Workshop  
@NTHU, June 15-18, 2026



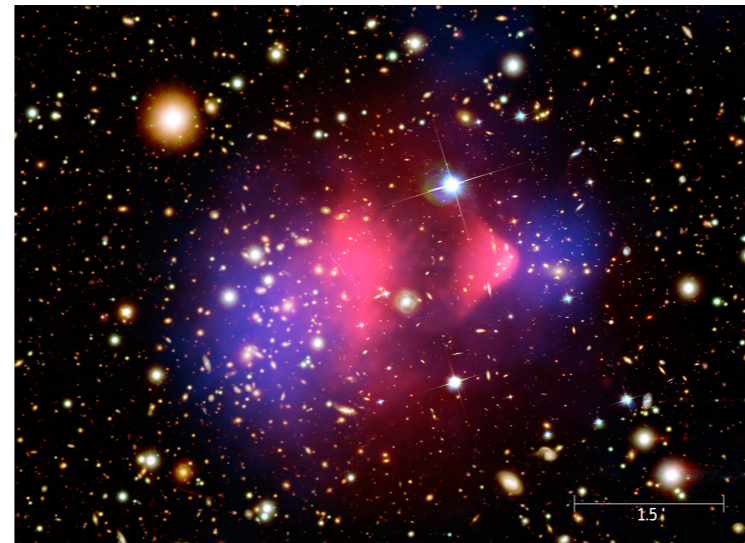
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Physics Division 國家理論科學研究中心 物理組



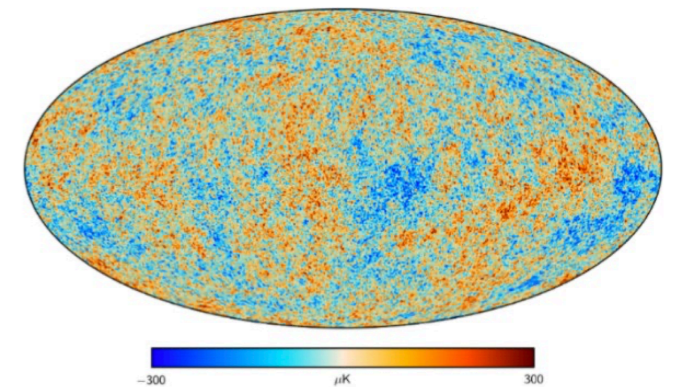
## Galactic rotation curve



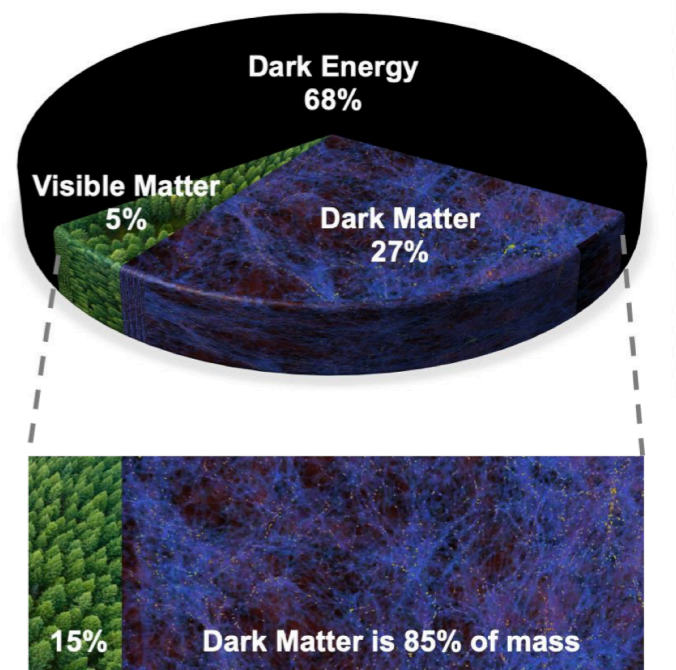
## Bullet Cluster



## CMB



- ◆ Many DM evidences due to its **gravitational effects**
- ◆ DM is the **dominant form** of matter in the Universe
- ◆ The nature of DM is still **a mystery!**





## ◆ Direct Detection

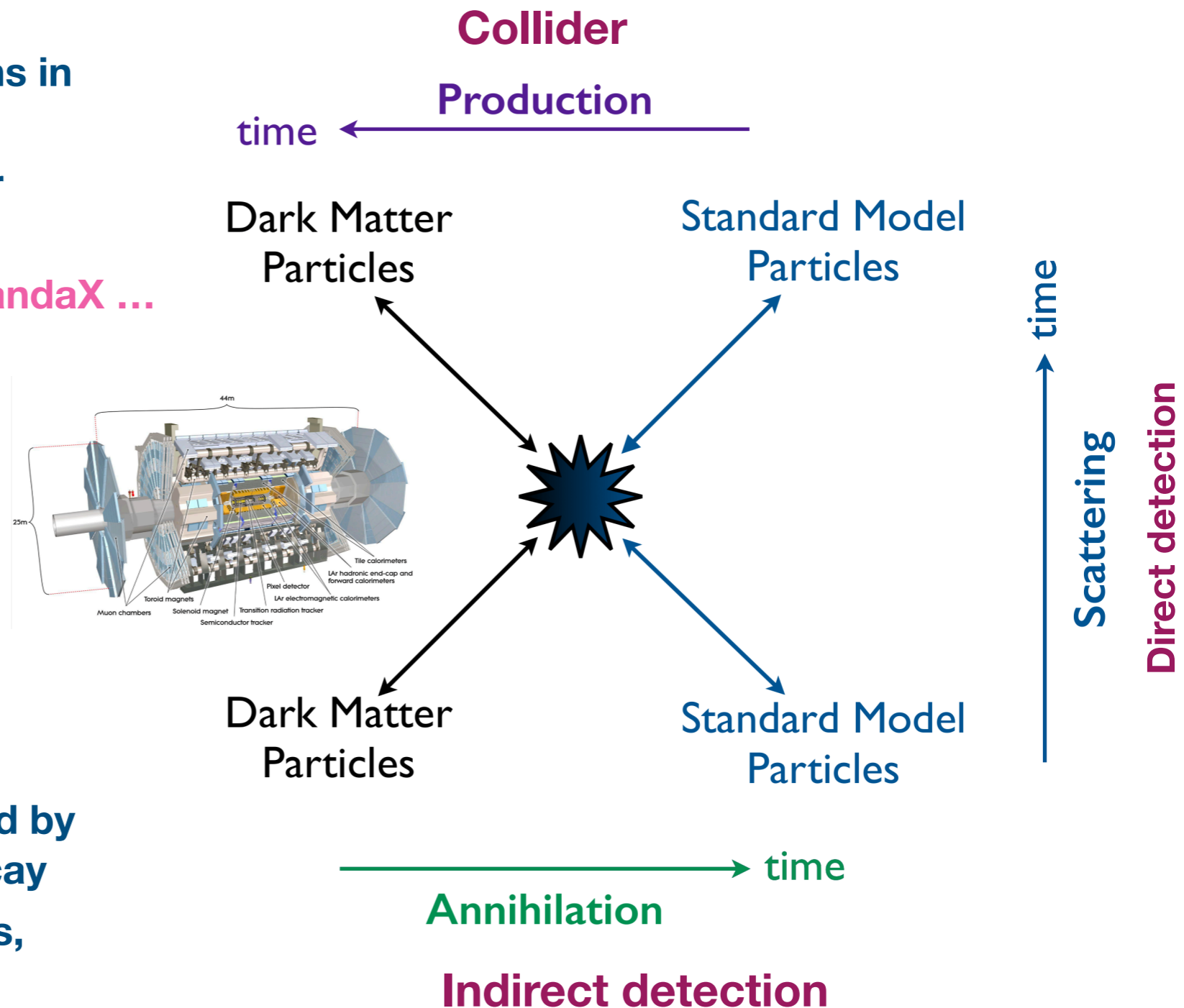
- DM scatters off nuclei/electrons in underground detectors
- Measure tiny nuclear recoils or ionization signals
- Experiments: XENON1T, LZ, PandaX ...

## ◆ Collider

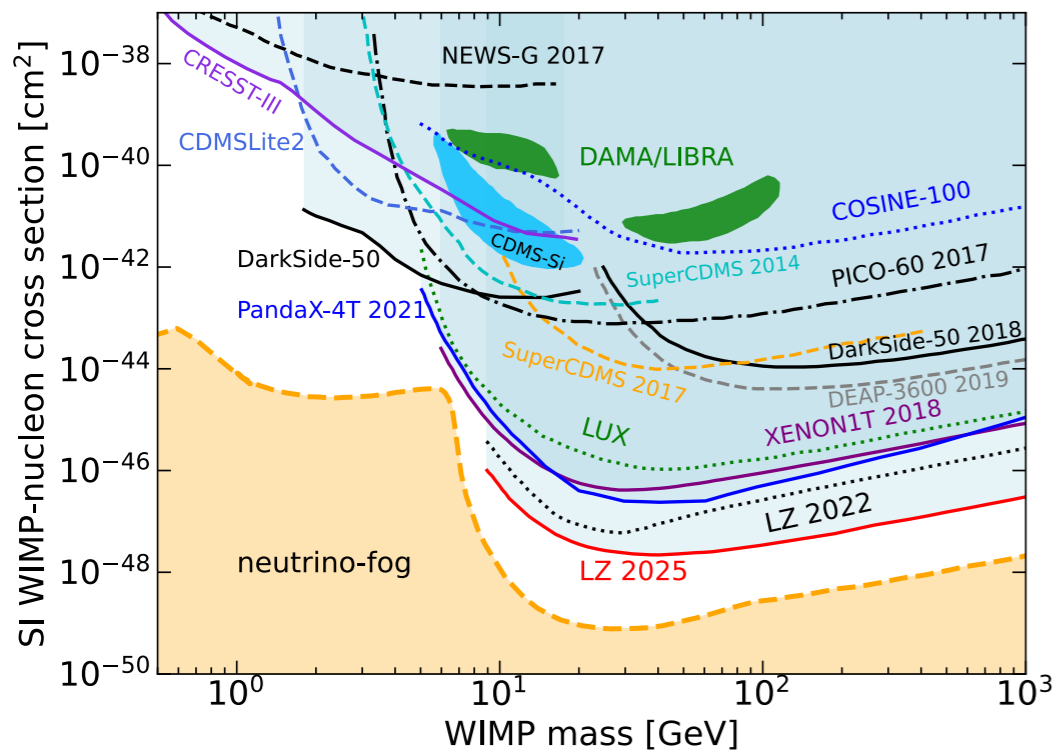
- Produce DM at high-energy collisions (e.g., LHC)
- Signature: missing transverse energy + visible particles (jets, photons, leptons)

## ◆ Indirect Detection

- Look for SM particles produced by dark matter annihilation or decay
- Signals: gamma rays, positrons, antiprotons, neutrinos
- Observatories: Fermi-LAT, AMS-02, IceCube, ...

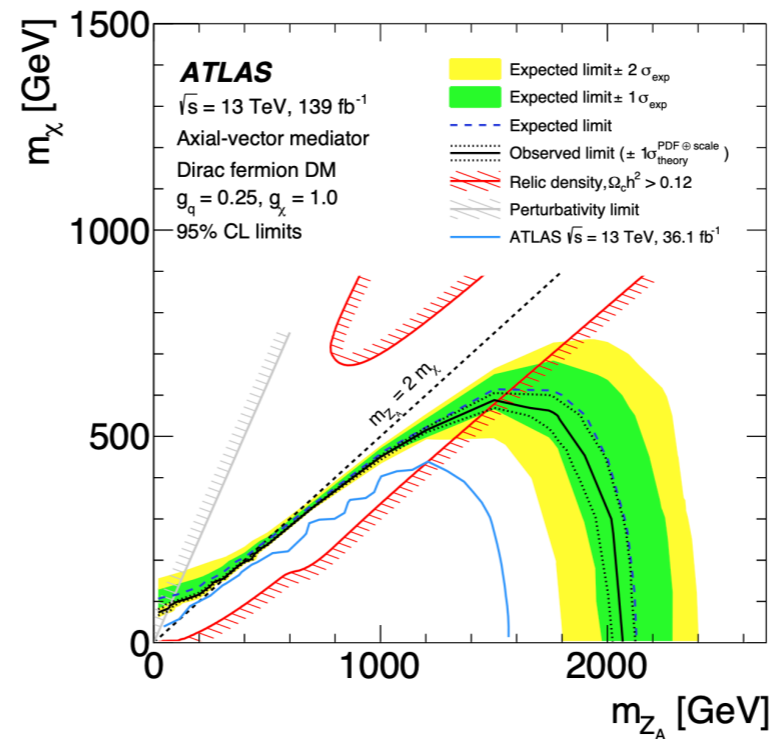


## Direct detection



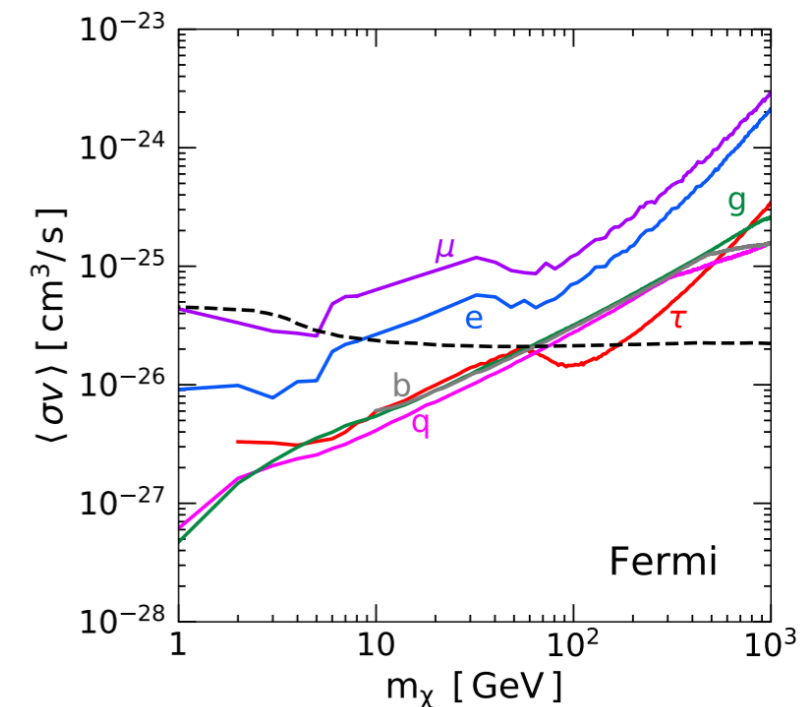
## Collider

PRD 103, 112006 (2021)



## Indirect detection

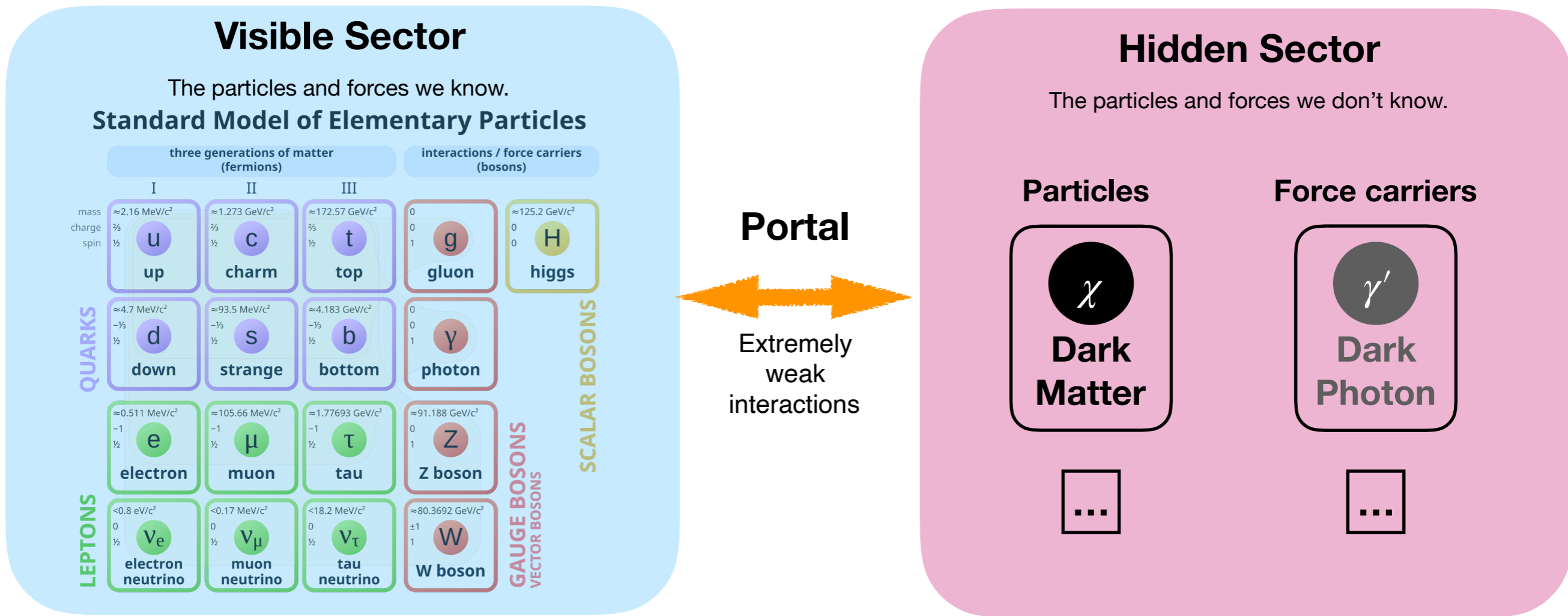
PRD 98, 023016 (2018)



- ◆ No signals from direct detection experiments
- ◆ No confirmed evidence at colliders
- ◆ No confirmed anomalous excesses from indirect detection



**Dark matter may interact very weakly to visible matter!**



- ◆ Our Universe may exist a **hidden world** which has the **Dark Matter** and its own forces
- ◆ This **Hidden world** interacts very feebly with the **visible world** via **portals**.

## ❖ Vector portal

$$\mathcal{L} \supset -\frac{\epsilon}{2} F'_{\mu\nu} F^{\mu\nu}$$

## ❖ Scalar portal

$$\mathcal{L} \supset \lambda_{HS} |H|^2 |S|^2$$

## ❖ Neutrino Portal

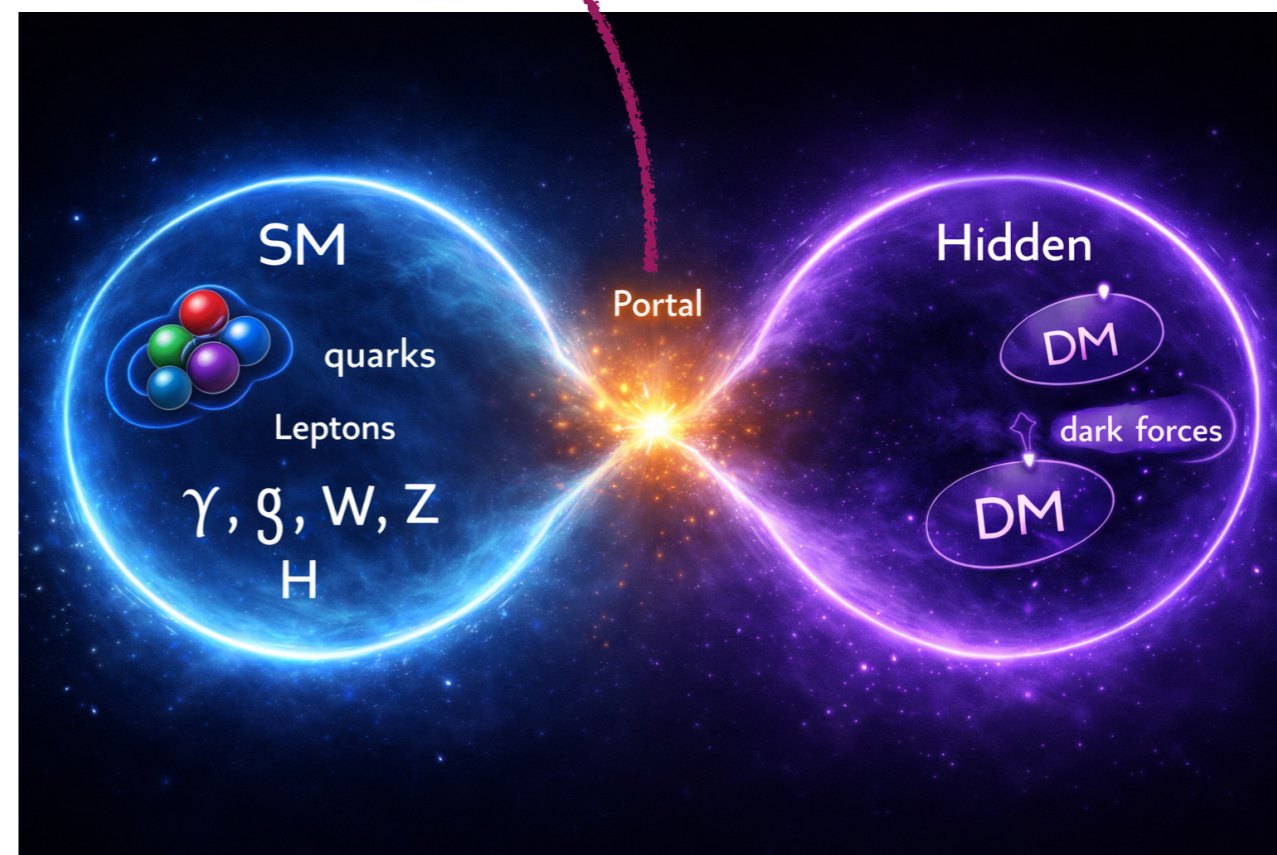
$$\mathcal{L} \supset y_N \bar{L} H N$$

## ❖ Axion (Pseudoscalar) Portal

$$\mathcal{L} \supset \frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

## ❖ Axion-Dark Photon Portal

$$\mathcal{L} \supset \frac{a}{f_a} F'_{\mu\nu} \tilde{F}^{\mu\nu}$$



## 1. U(1) kinetic mixing

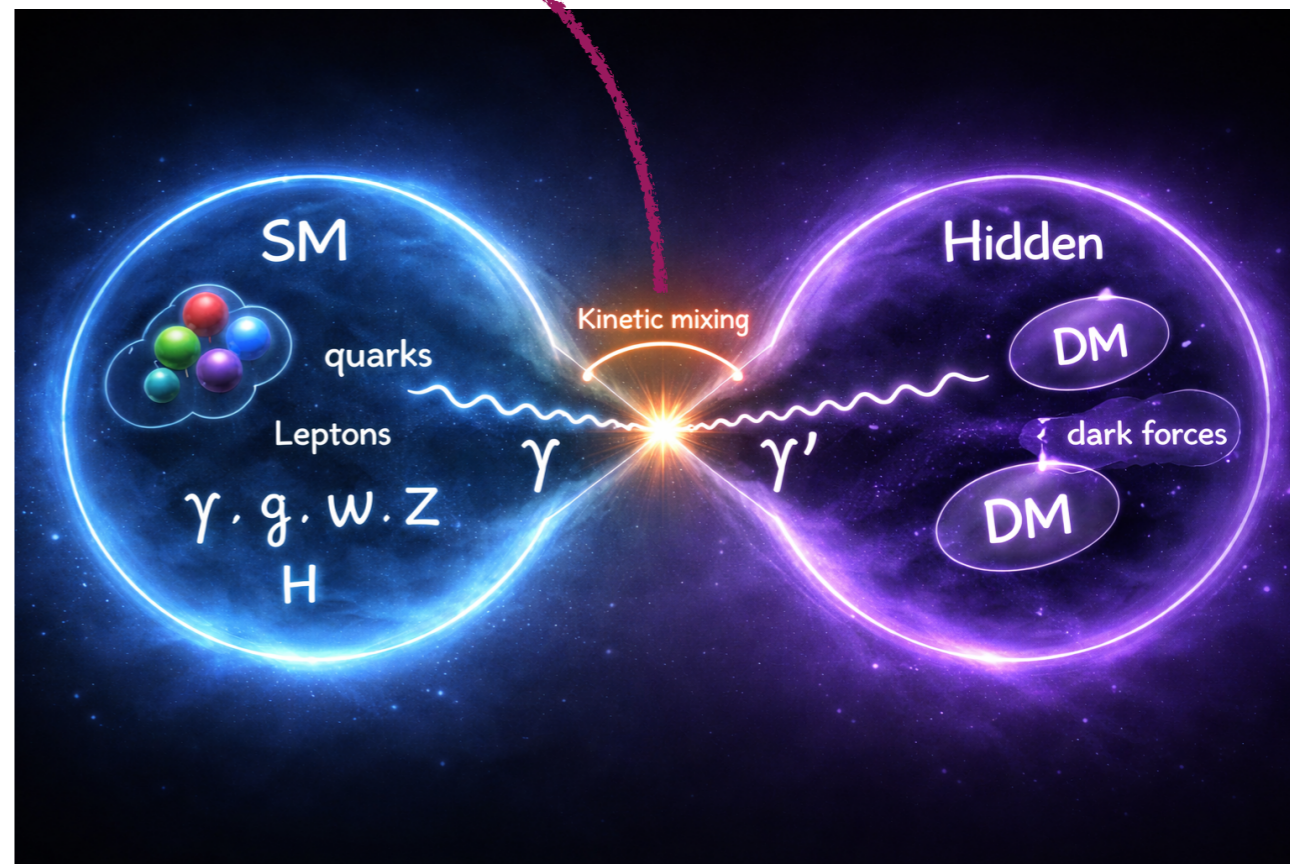
$$\mathcal{L} \supset -\frac{\epsilon}{2} F'_{\mu\nu} F^{\mu\nu}$$

Holdom (1986), +++

## 2. U(1) Stueckelberg mass mixing

$$\mathcal{L} \supset -\frac{1}{2} (\partial\sigma + m_1 \epsilon B_\mu + m_1 X_\mu)^2$$

D. Feldman, Z. Liu, and P. Nath (2006), +++



## 3. Abelian – Non-Abelian kinetic mixing

$$\mathcal{L} \supset -\frac{\epsilon}{2} W_D^{3\mu\nu} B_{\mu\nu}$$

Arised from the dim-5/dim-6 operator

$$\mathcal{O}_5 = \frac{c_5}{\Lambda} \text{Tr} \left[ \Sigma W_D^{\mu\nu} \right] B_{\mu\nu},$$

$$\mathcal{O}_6 = \frac{c_6}{\Lambda^2} (\Phi^\dagger \sigma^a \Phi) W_{\mu\nu}^a B^{\mu\nu}$$

VQT and Tzu-Chiang Yuan (2024, 2025)  
P. Ko, Takaaki Nomura, Hiroshi Okada (2021)

G. Barello, Spencer Chang, Christopher A. Newby (2015),  
C.A. Argüelles, X-G. He, G. Ovanessian, T. Peng, Michael J. Ramsey-Musolf (2017)



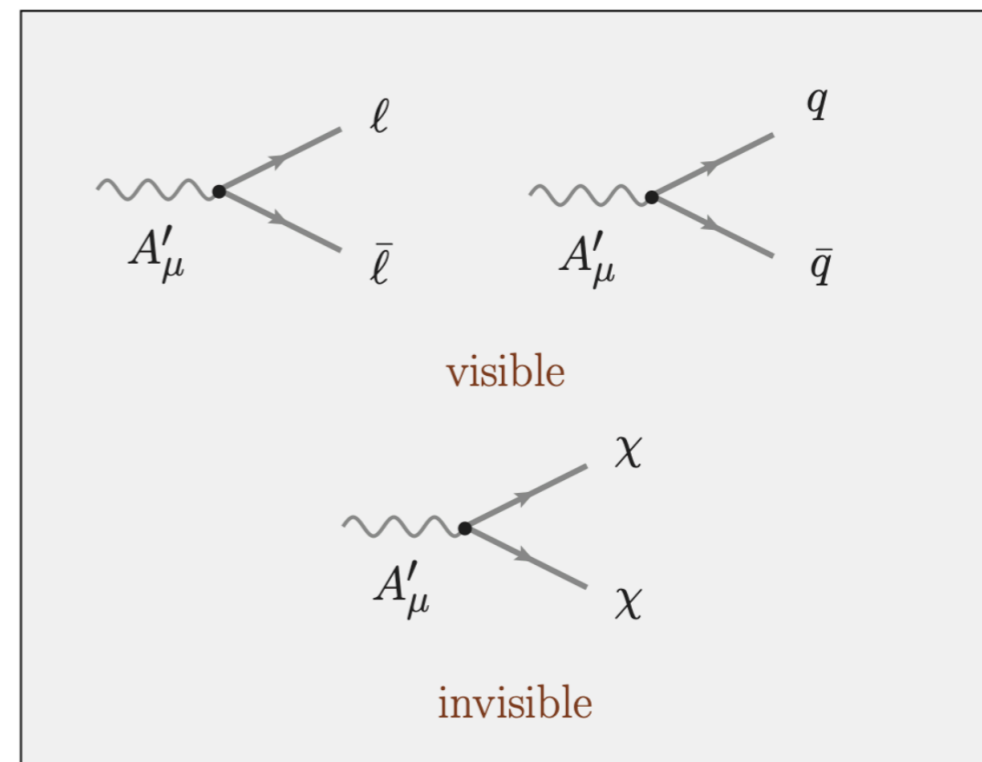
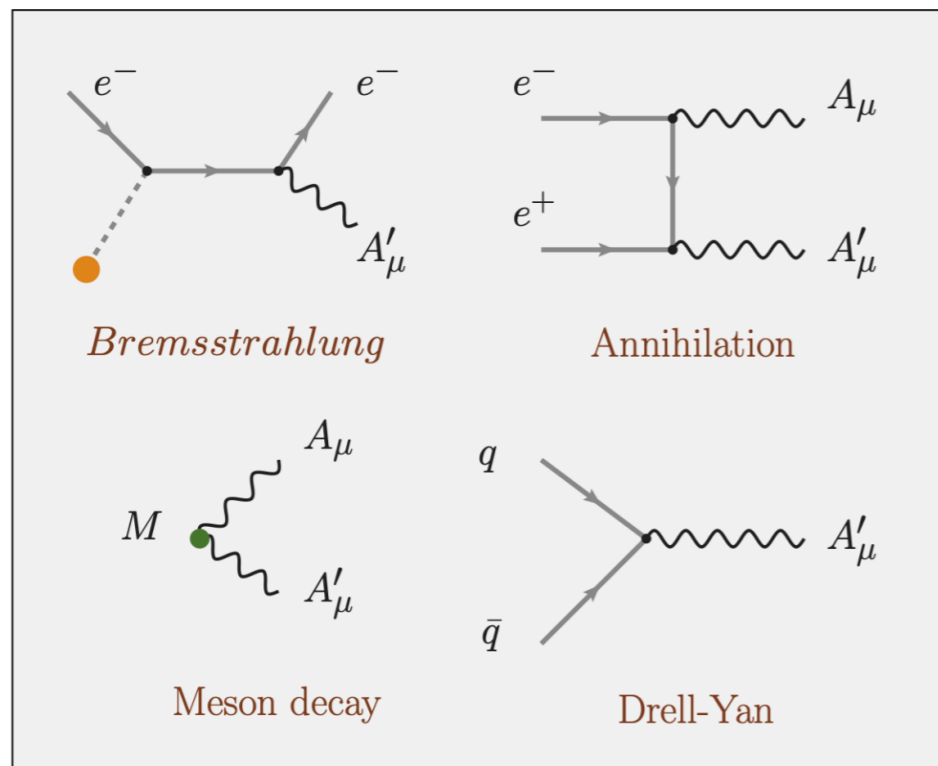
# Searches for Massive Dark Photons

- ◆ The interaction between a dark photon  $A'_\mu$  to SM particle is controlled by the parameter  $\epsilon$

$$\mathcal{L} = \epsilon e J^\mu A'_\mu$$

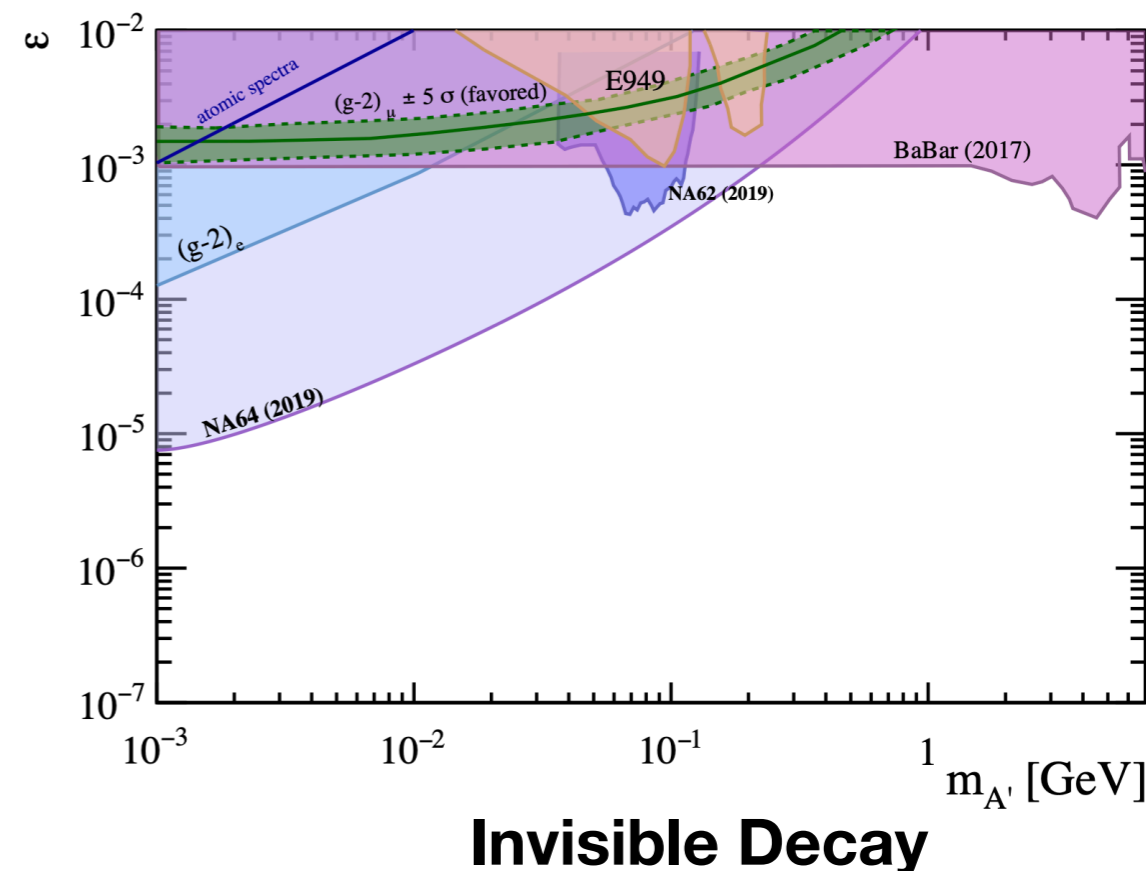
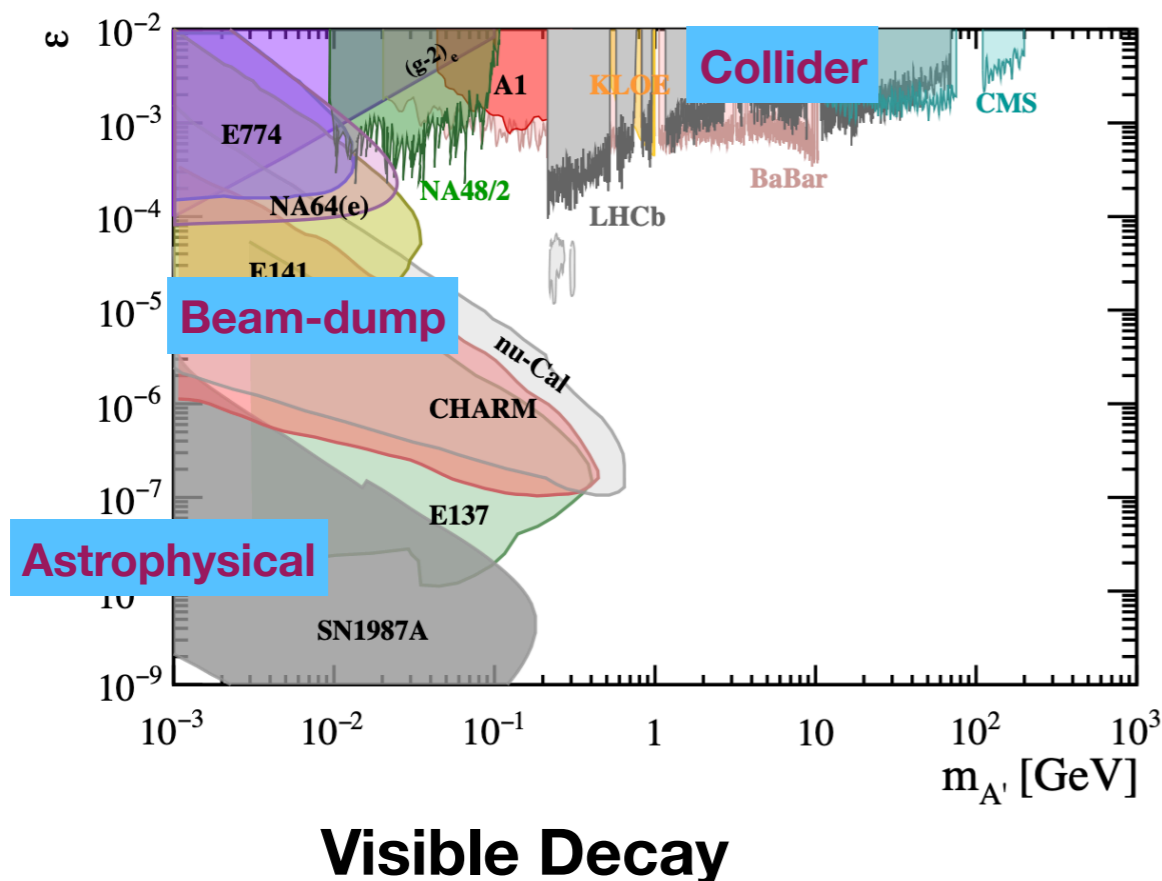
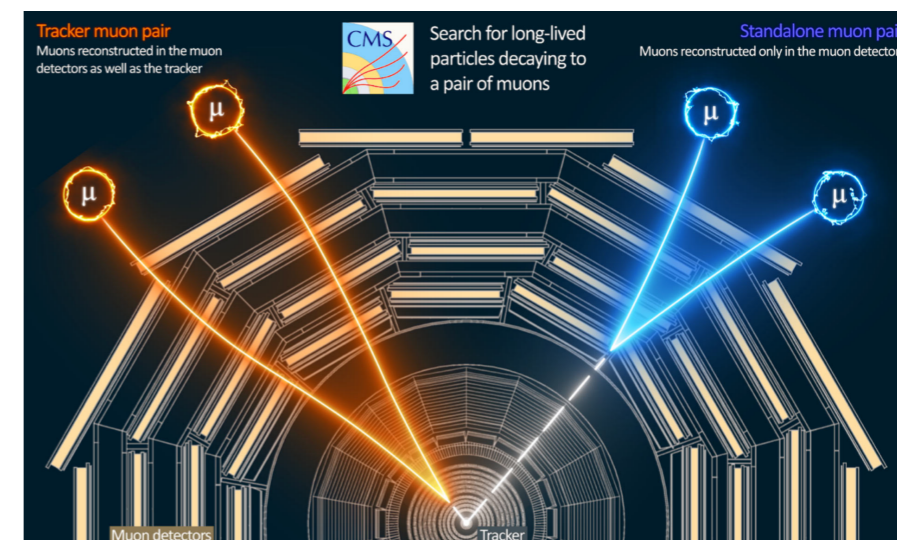
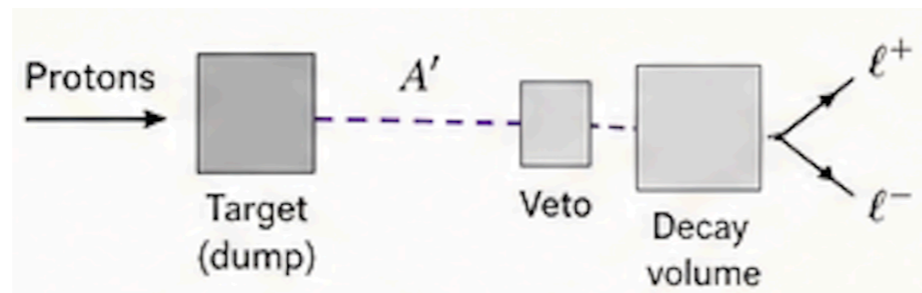
The electromagnetic current

- ◆ Production and Decay channels:

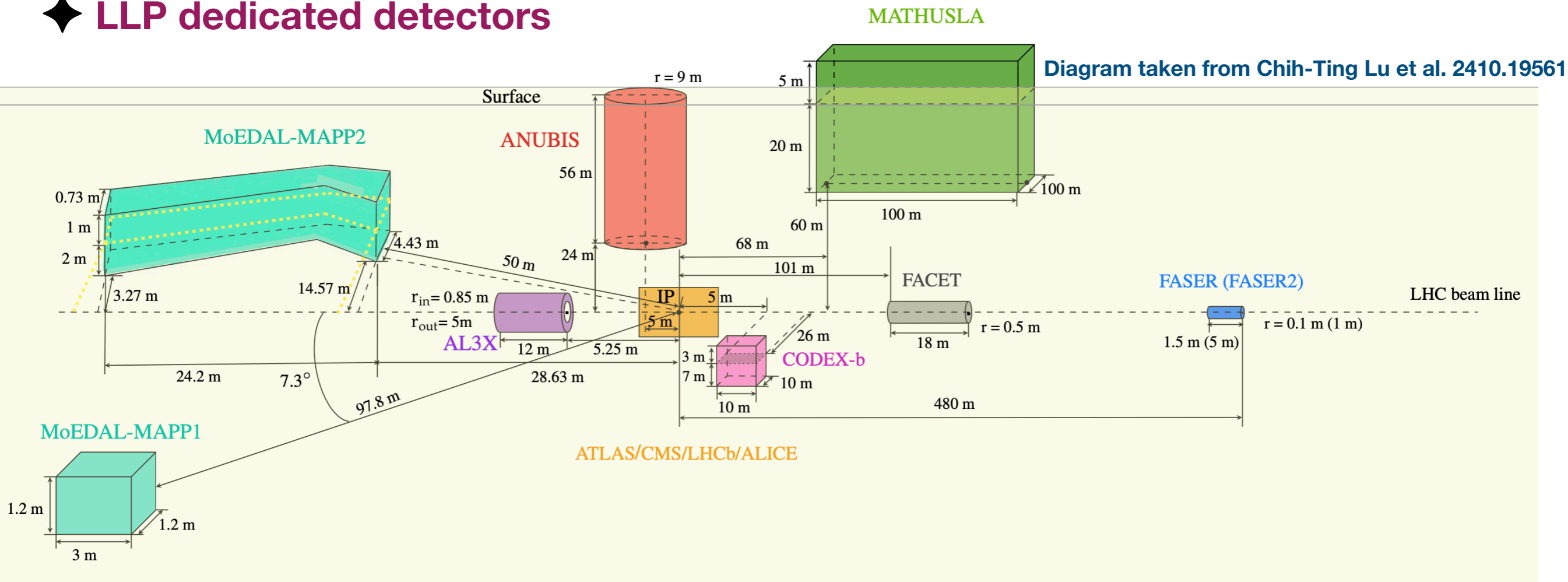


◆ **Colliders:** Search for resonances in the invariant mass distribution of  $e^+e^-$  or  $\mu^+\mu^-$  pairs

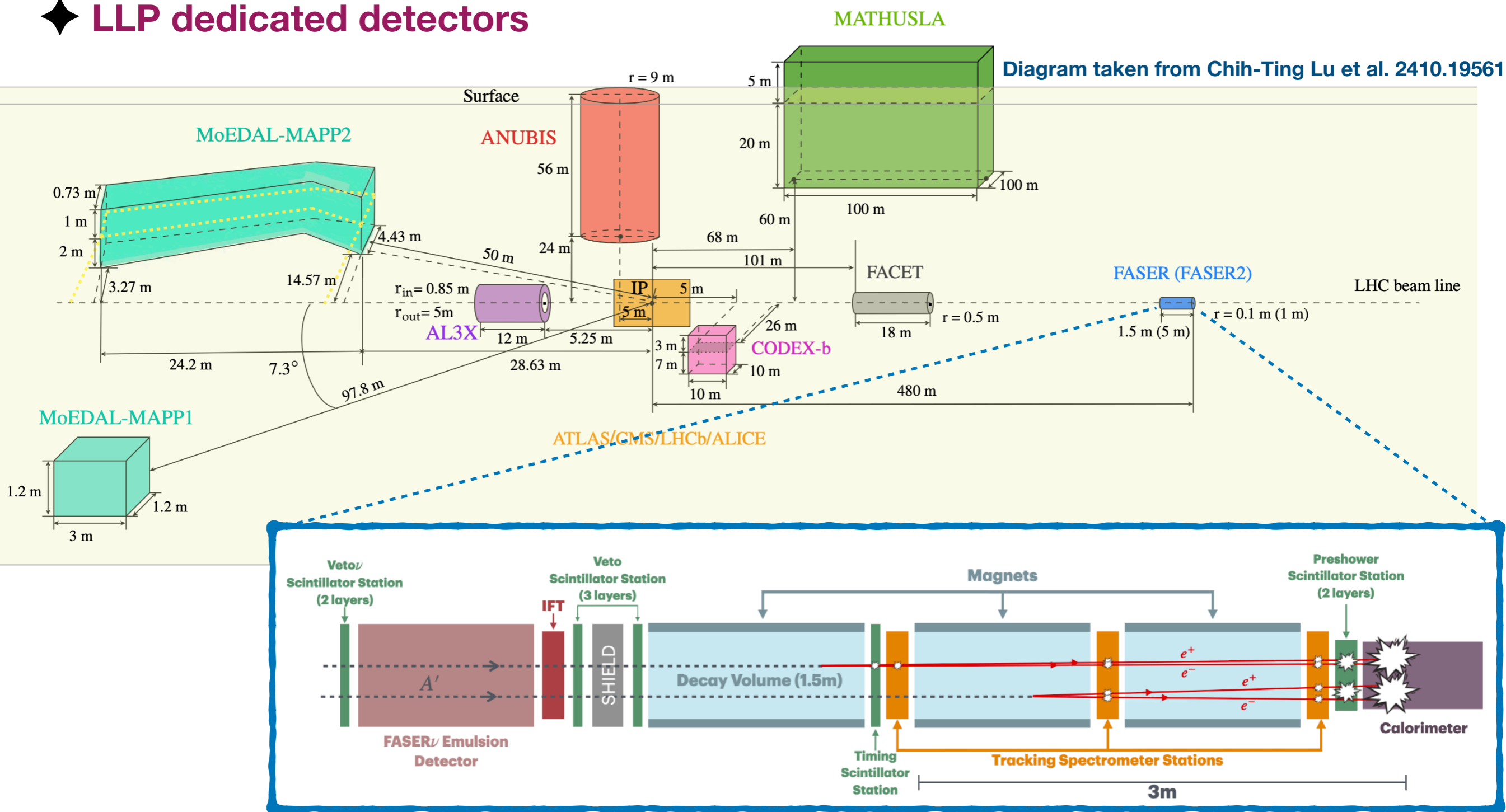
◆ **Beam-dump/Fix target experiments:** shooting electron or proton beam to a fixed-target or a dump to generate the dark photon



## LLP dedicated detectors

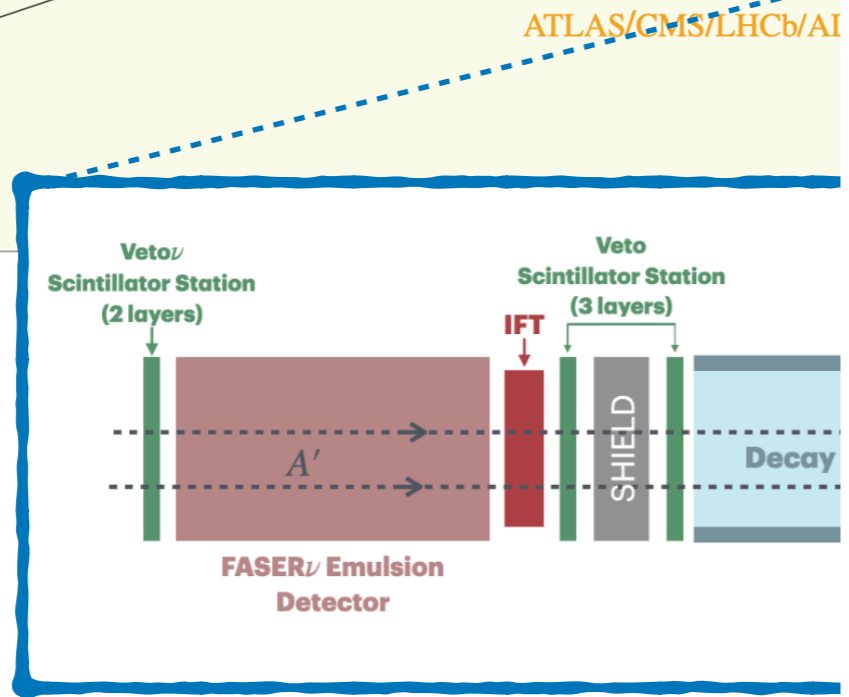
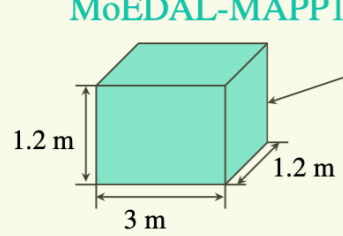
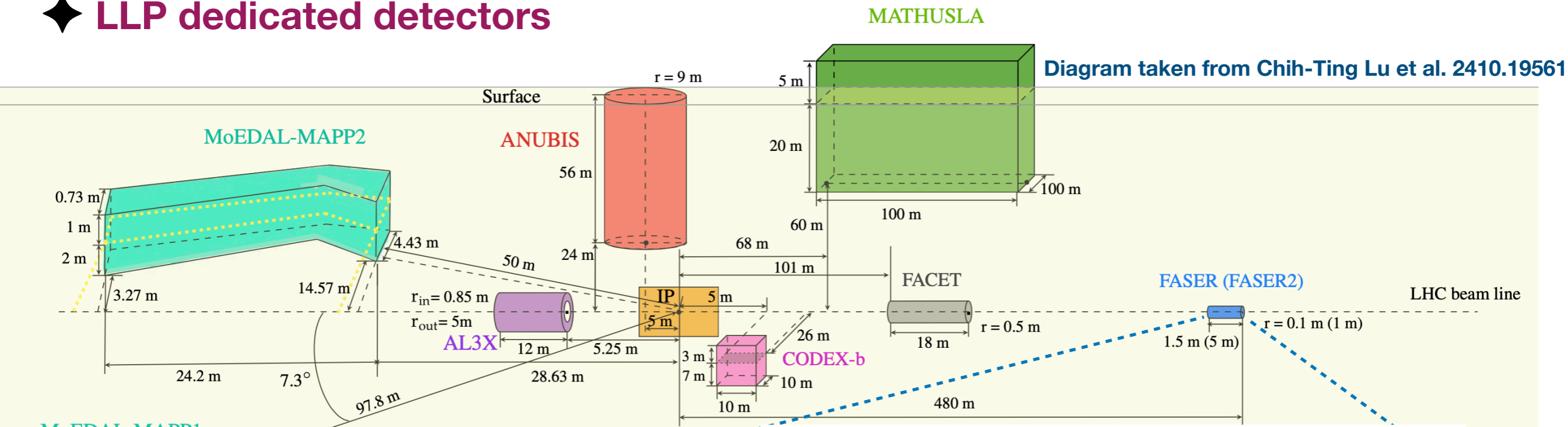


## LLP dedicated detectors

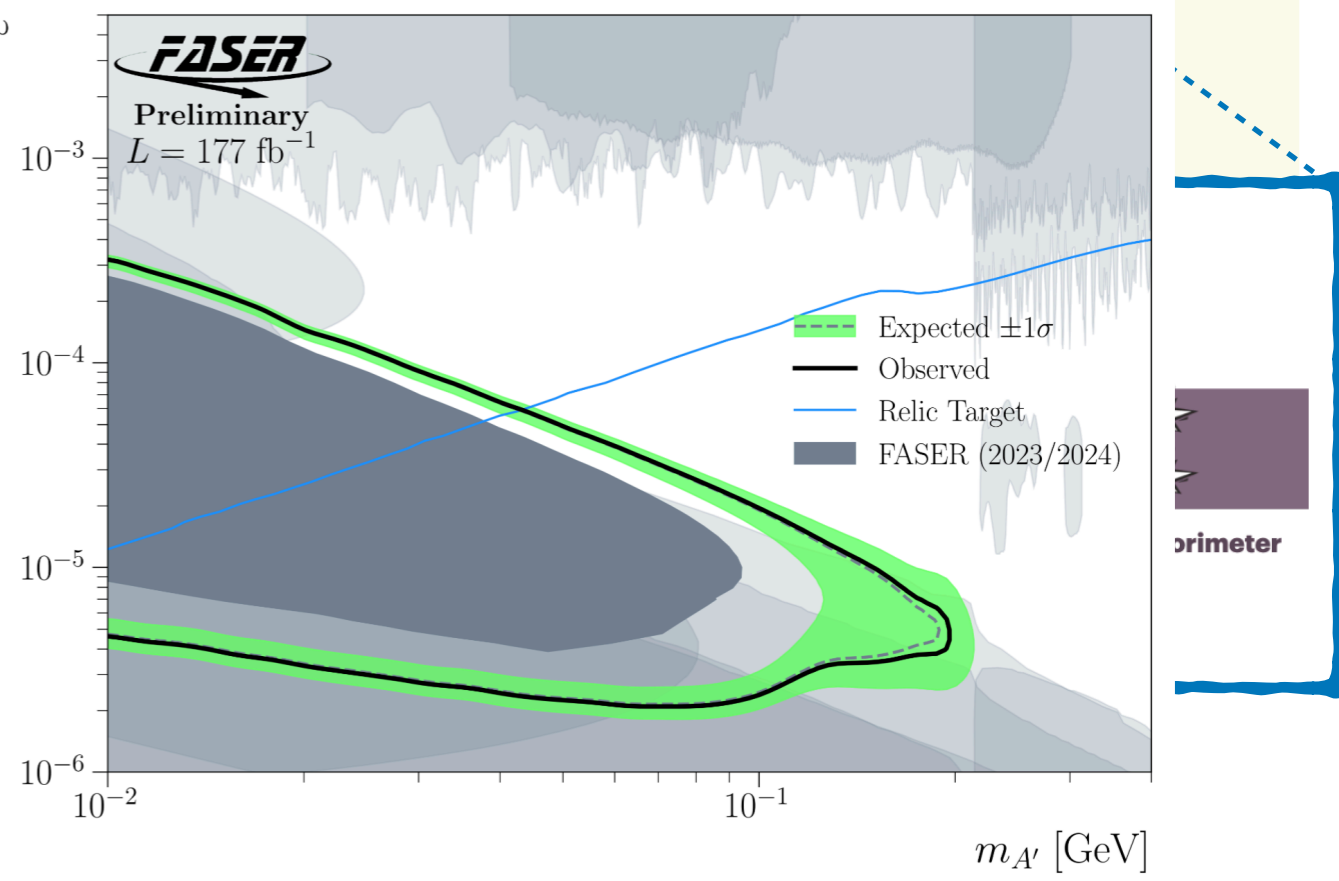


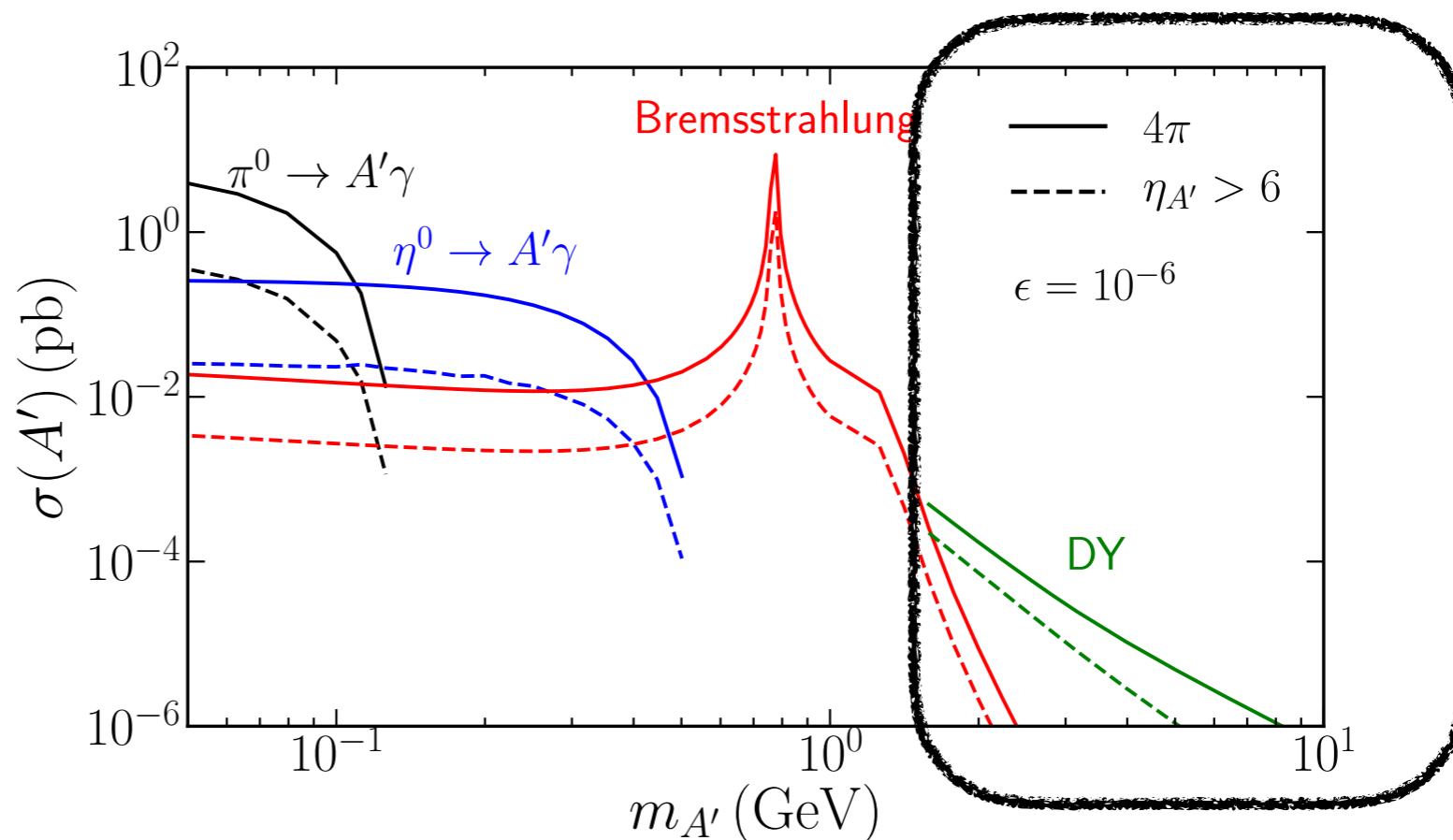
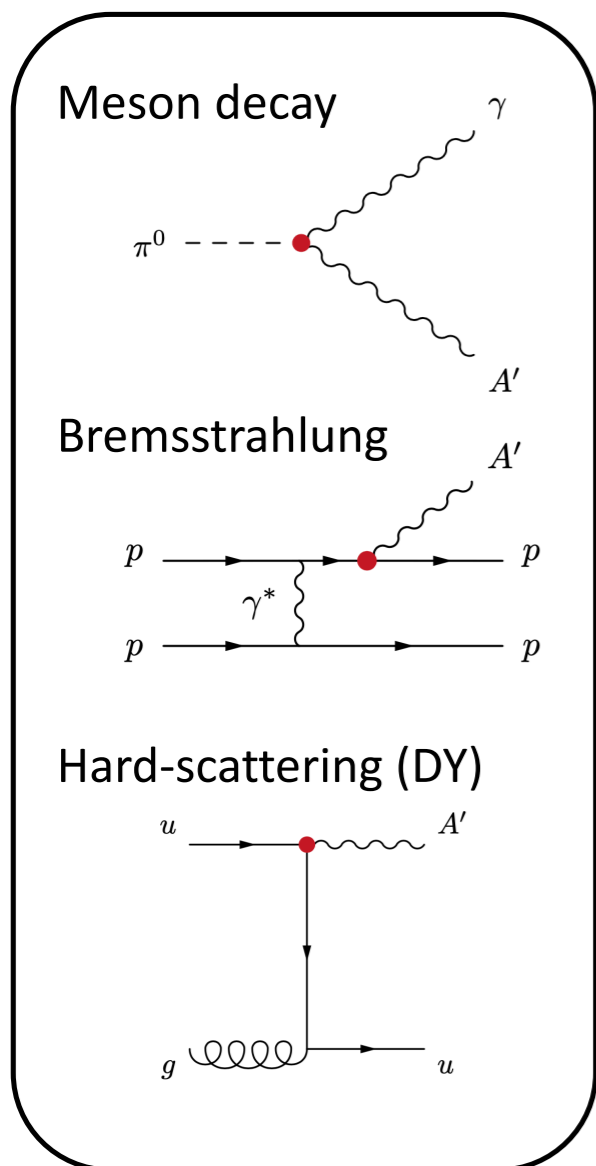
<https://faser.web.cern.ch/briefing-20260319>

## LLP dedicated detectors



<https://faser.web.cern.ch/briefing-20260319>

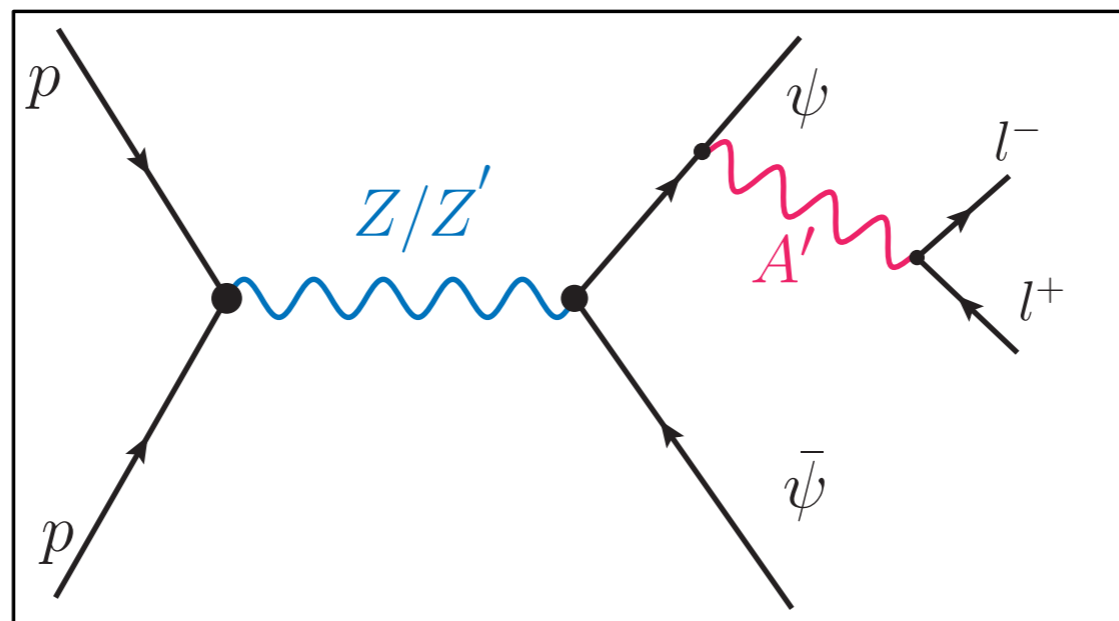




- ❖ **For low mass region**, the meson decays and Bremsstrahlung processes are dominant
- ❖ **For DP mass  $> 1.5$  GeV**, the hard-scattering process becomes dominant but the **cross section is suppressed**.
- ❖ **Only about 10%** of total DP produced in the **very forward region**.

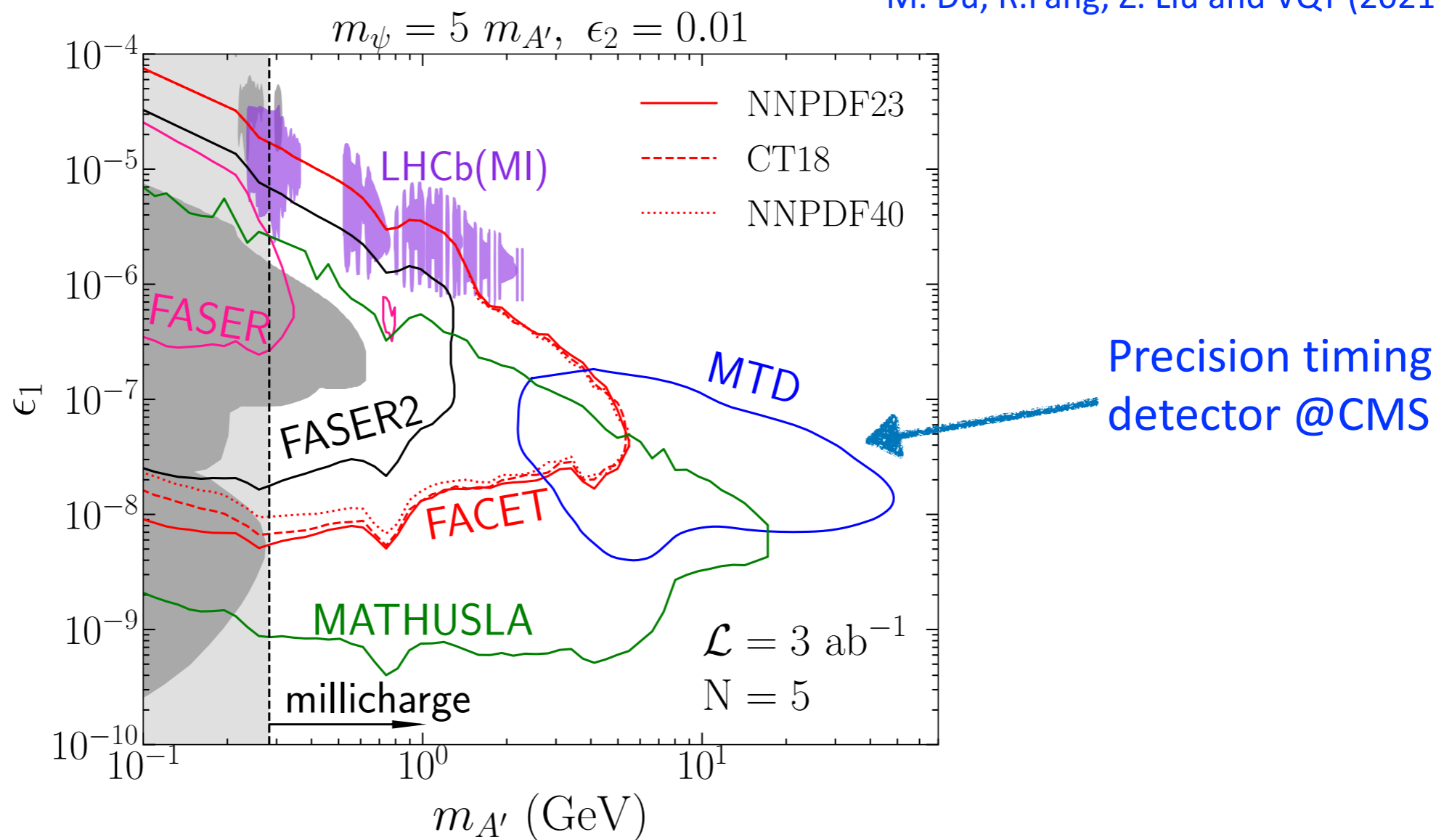
❖ **If future detectors observe LLDP signals with a higher mass region, there must be something beyond this conventional DP model!**

- ◆ Dark matter is produced via  $Z$  or  $Z'$  mediators at  $pp$  collision and then radiates dark photons



- ◆ A crucial feature: production and decay of dark photon can be separated

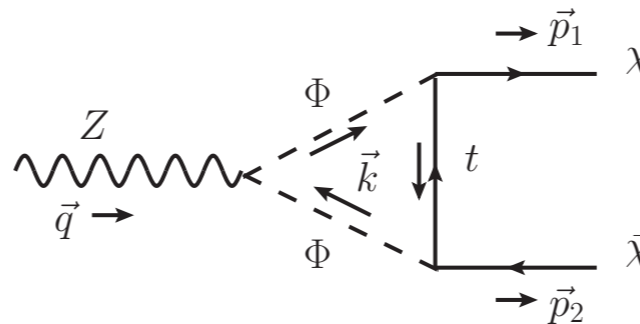
M. Du, R.Fang, Z. Liu and VQT (2021)



Precision timing and dedicated LLP detectors can **complementarily** search for DP at mass  $\sim O(10 \text{ GeV})$

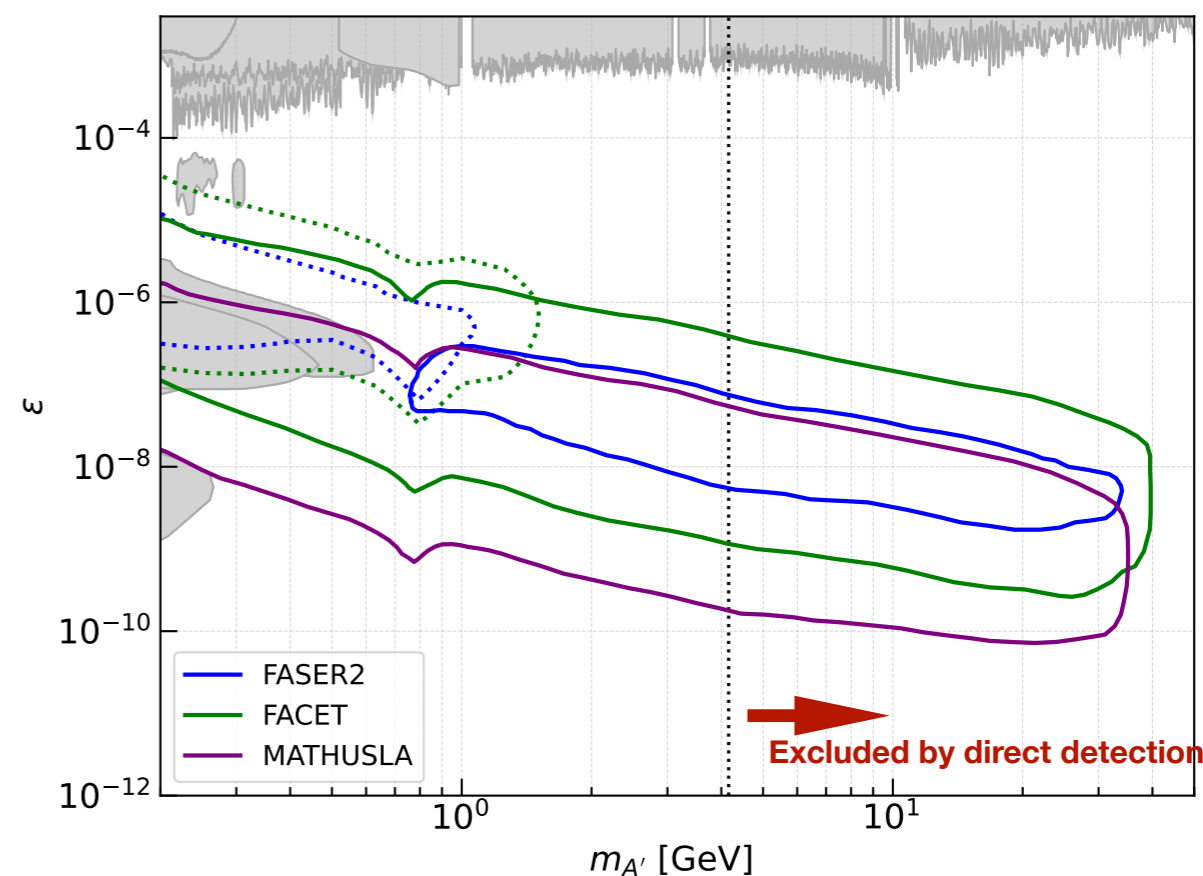
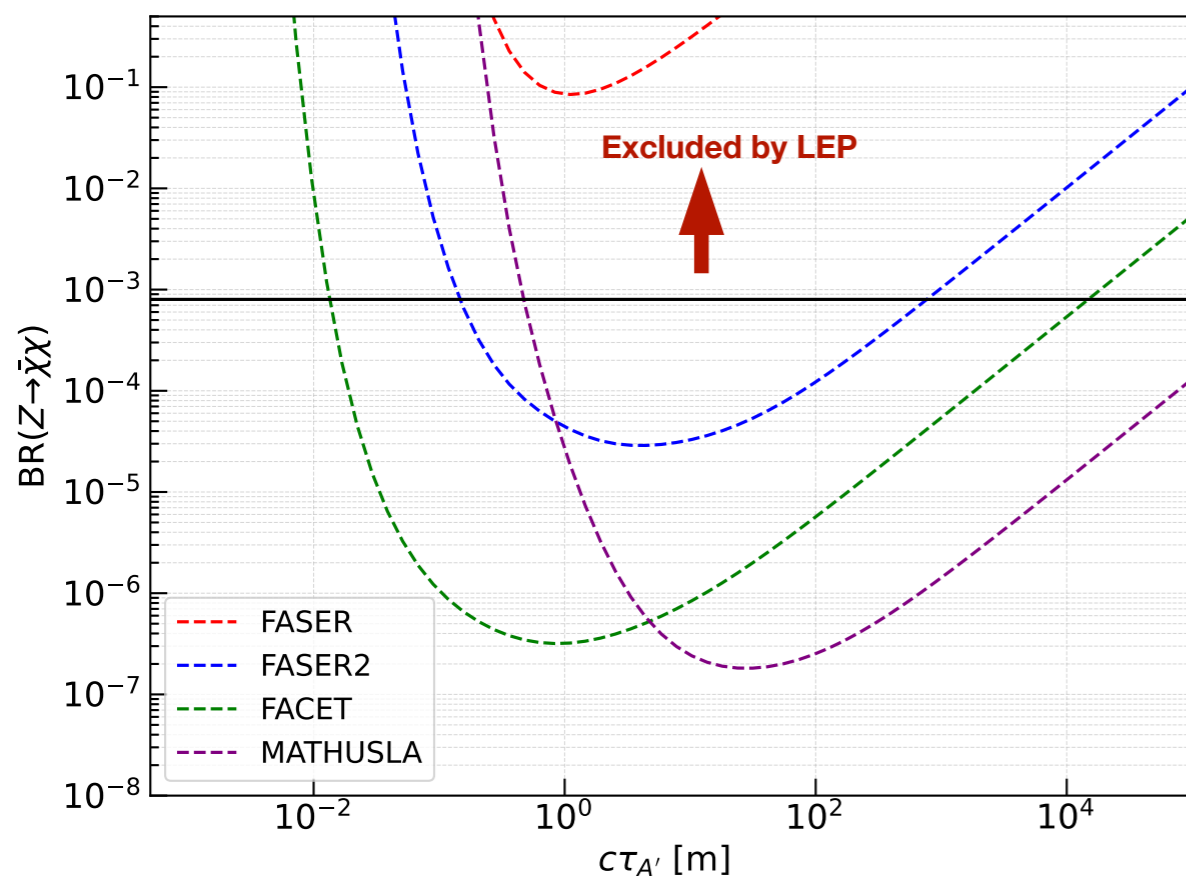


# Z decay model



$$m_\chi = 2 \text{ GeV}, \Delta = \frac{m_{A'} - m_\chi}{m_\chi} = 0.3 \text{ and } \alpha_D \simeq 0.23$$

$$\Delta = 0.3 \text{ and } \text{BR}(Z \rightarrow \tilde{\chi}\chi) = 10^{-4}$$



- ❖ Solid lines: production from HR channel
- ❖ Dotted lines: conventional production channels

C.R.Chen, VQT, arXiv:2605.03427

- ❖ FASER alone does not surpass the current Z invisible width bound
- ❖ Future FASER2, FACET, and MATHUSLA **improve significantly** and can probe the parameter space **beyond** that in the conventional DP model.



# A non-Abelian Dark Sector

- ◆ Dark sector consists a non-Abelian gauge group

$$G_{\text{SM}} \otimes SU(2)_D$$

- ◆ Abelian–Non-Abelian kinetic mixing as the portal

$$\mathcal{L} \supset -\frac{\epsilon}{2} W_D^{3\mu\nu} B_{\mu\nu}$$

- ◆ The non-Abelian charged gauge bosons can be DM:

- ❖ Its stability can be ensured by **a gauge symmetry**
- ❖ **Intrinsic self-interacting** with long range dark photon -> can address **small scale problems (core-cusp, too big to fail, missing satellites) (1)**
- ❖ **Feebly interaction with SM** -> e.g. via kinetic mixing -> DM relic abundance can be realized by **freeze-in mechanism**
- ❖ **A millicharged particle**

(1) S. Tulin and H. B. Yu (2018), VQT, Nguyen, and Yuan, JCAP 05 (2024) 015; +++

- ◆ SM is enlarged with a **dark gauge sector**  $SU(2)_D$  broken by a **real dark triplet Higgs**  $\Sigma$

$$\Sigma = \frac{1}{2} \Sigma^a \sigma^a = \frac{1}{2} \begin{pmatrix} \Sigma^0 + v_\Sigma & \sqrt{2} \Sigma^p \\ \sqrt{2} \Sigma^m & -\Sigma^0 - v_\Sigma \end{pmatrix}$$

- ◆ After the breaking of  $SU(2)_D \rightarrow U(1)_D$ , the **charged dark vectors**  $W_\mu^{p,m} = \frac{1}{\sqrt{2}} (W_{D\mu}^1 \mp i W_{D\mu}^2)$  obtain a mass  $m_{W^{p,m}} = g_D v_\Sigma$  and being **DM candidate**.

The  $U(1)_D$  charge ensures the DM stable

- ◆ The **neutral dark vector**  $W_{D\mu}^3$  is **massless** (denoted as  $Z'$  in physical state)

- ◆ Dimension 5 operator induces Dimension 4 kinetic mixing term:

$$\mathcal{O}_5 = \frac{c_5 g_D g'}{\Lambda} \text{Tr} \left[ \Sigma W_D^{\mu\nu} \right] B_{\mu\nu} \xrightarrow{\langle \Sigma \rangle} -\frac{1}{2} \epsilon W_D^{3\mu\nu} B_{\mu\nu}$$

with  $\epsilon = -\frac{c_5 g_D g' v_\Sigma}{\Lambda}$  referred as **Abelian–Non-Abelian kinetic mixing**.

- ◆ The kinetic energy of the gauge sector in the extended model is

$$\mathcal{L}_{\text{kin}} = -\frac{1}{4}B_{\mu\nu}B^{\mu\nu} - \frac{1}{4}W_{\mu\nu}^a W^{a\mu\nu} - \frac{1}{4}W_{D\mu\nu}^a W_D^{a\mu\nu} - \frac{1}{2}\epsilon W_D^{3\mu\nu} B_{\mu\nu}$$

- ◆ Diagonalization of the kinetic terms

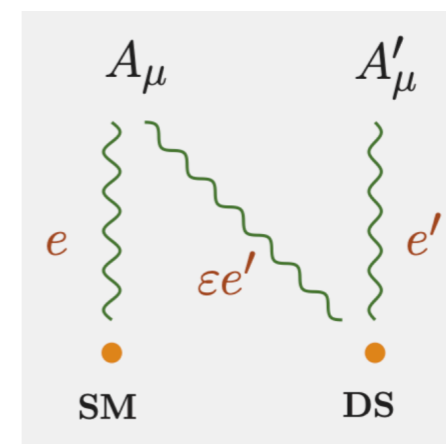
$$\begin{pmatrix} W_{D\mu}^3 \\ B_\mu \end{pmatrix} \rightarrow \begin{pmatrix} 1 & \frac{-\epsilon}{\sqrt{1-\epsilon^2}} \\ 0 & \frac{1}{\sqrt{1-\epsilon^2}} \end{pmatrix} \cdot \begin{pmatrix} c_\alpha & -s_\alpha \\ s_\alpha & c_\alpha \end{pmatrix} \cdot \begin{pmatrix} W_{D\mu}^3 \\ B_\mu \end{pmatrix}$$

- ❖ Physical observables must be independent of  $\alpha$  as it reflects a redundancy in the choice of basis in the unbroken Abelian subgroup  $U(1)_Y \times U(1)_D$

J.-X. Pan, M. He, X.-G. He, and G. Li, NPB 953, 114968 (2020)

- ◆ We adopt the *millicharged basis* defined by

$$s_\alpha = \epsilon, \quad c_\alpha = \sqrt{1-\epsilon^2}$$



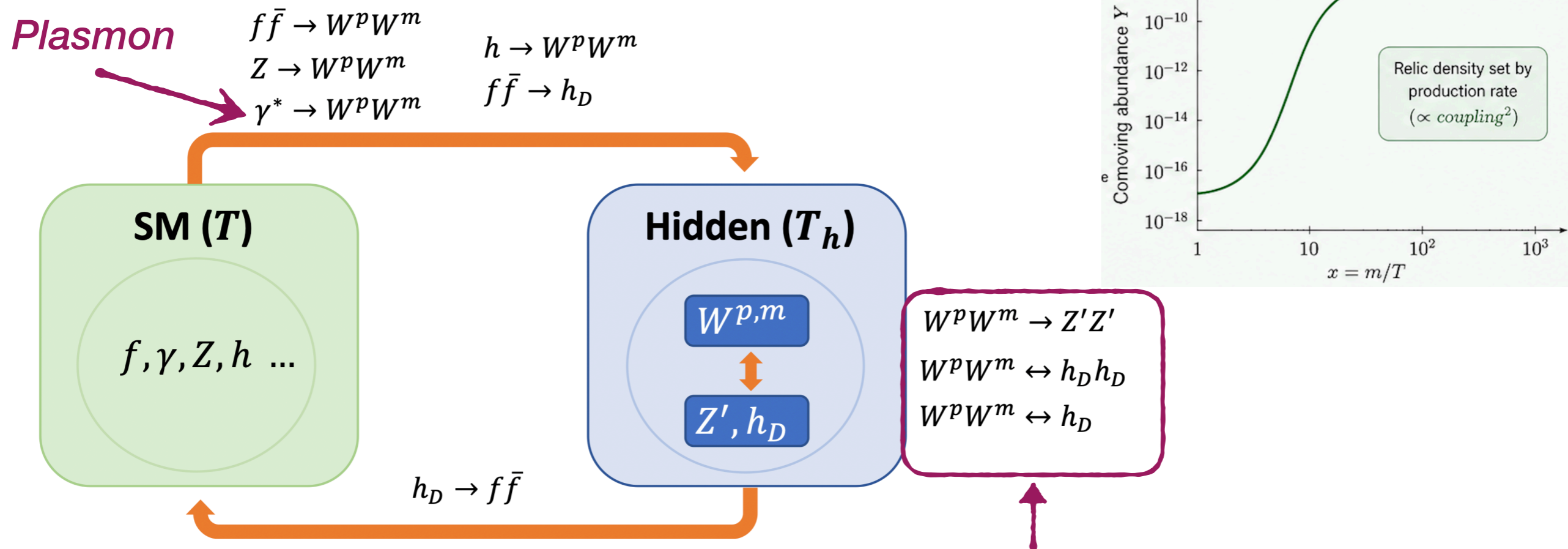
- ◆ The kinetic mixing diagonalization also induces couplings of DM candidate  $W^{(p,m)}$  to physical photon

$$\mathcal{L}_{\text{milli}} \supset -ig_D \cos \theta_W \epsilon \left( W_{\mu\nu}^p W^{m\mu} - W_{\mu\nu}^m W^{p\mu} \right) A^\nu$$

 Dark matter is a millicharged particle!

# Freeze-in production framework

- ◆ Dark sector is **feebly interacting** with the SM visible sector: **kinetic mixing** and **Higgs mixing**
- ◆ SM sector and dark sector are **two distinct heat baths** with different temperature  $T$  and  $T_h$  and a ratio  $\xi \equiv T_h/T$  (1)



**Strong DS interactions deplete DM abundance**

(1) Aboubrabim et al, PRD 103, 075014 (2021); JHEP 09 (2022) 084; JHEP 12 (2021) 148; JHEP 06 (2021) 086; Feng, Li & Nath, PRD 110, 015020 (2024); Li & Nath, PRD 111 (2025) 12, 123007; LHEP 2024 (2024) 502; +++

## ◆ Temperature evolution

$$\frac{d\xi}{dT} = \frac{1}{T} \left[ -\xi + \left( \frac{3H(\rho_h + p_h) - J_h}{3H(\rho_v + p_v) + J_h} \right) \frac{d\rho_v}{dT} \left( \frac{d\rho_h}{dT} \right)^{-1} \right] \quad \xi \equiv \frac{T_h}{T}$$

where  $H$  is the Hubble parameter, and  $\rho_{v,h}$  and  $p_{v,h}$  are the energy and pressure densities of the visible and hidden sectors. The source function  $J_h$  encodes all **energy-exchange processes between the two sectors**

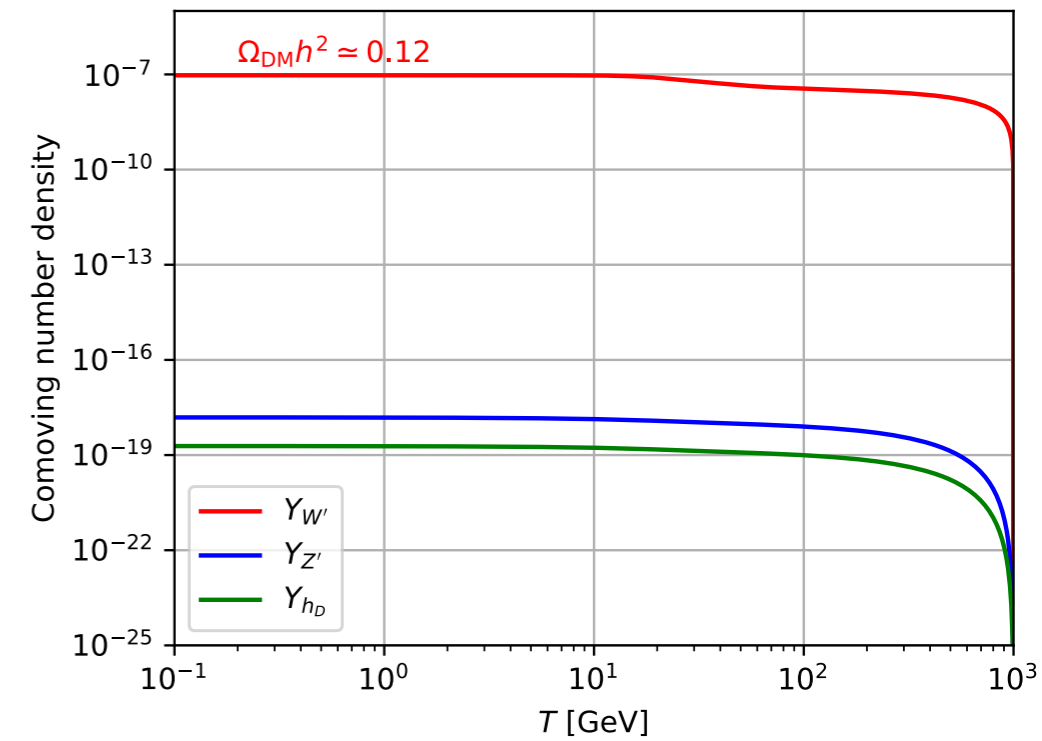
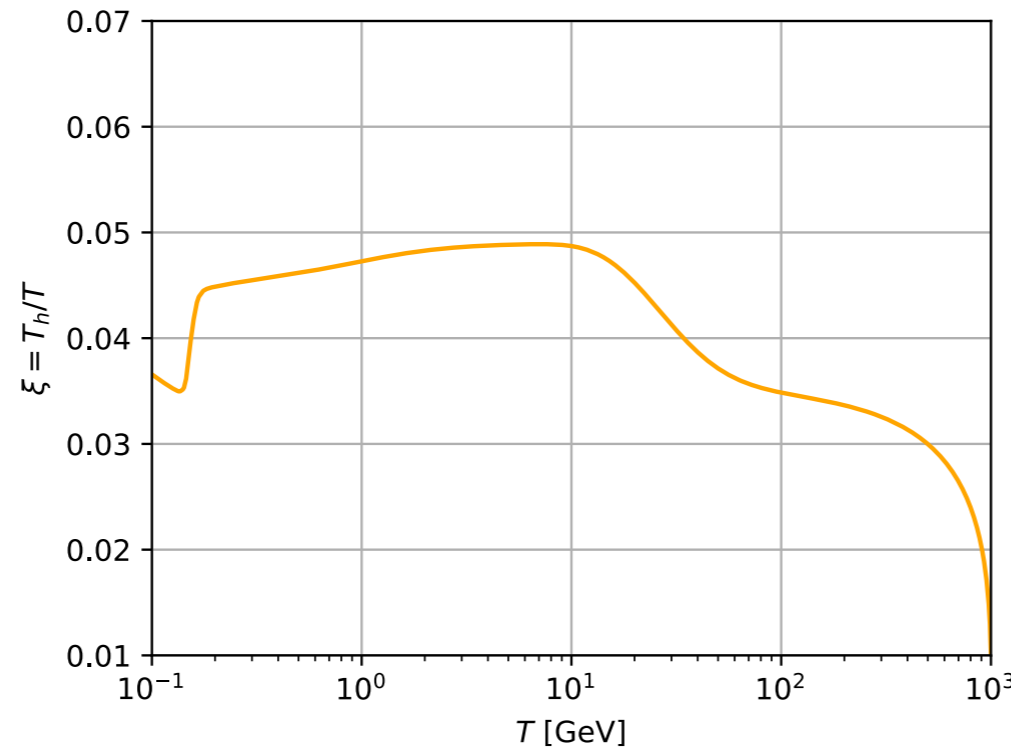
## ◆ Comoving yields evolution $Y_i = n_i/s$

$$\frac{dY_i}{dT} = -\frac{1}{s} \left[ \frac{d\rho_v/dT}{3H(\rho_v + p_v) + J_h} \right] \mathcal{R}_i(T, T_h), \quad i = W', Z', h_D$$

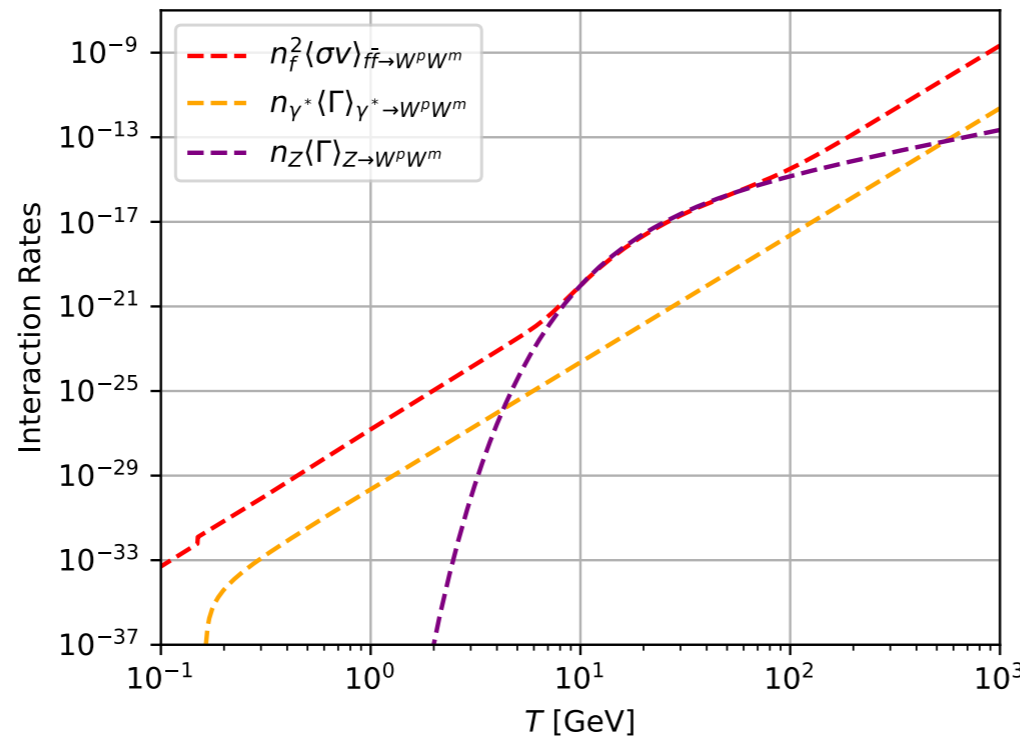
where  $s$  is the total entropy density,  $n_i$  the number density, and  $\mathcal{R}_i(T, T_h)$  the **interaction rate producing species  $i$** , including all three **SM to hidden, hidden to SM, and hidden to hidden channels**

BM :  $m_{W'} = 0.01$  GeV,  $m_{h_D} = m_{W'}/3$ ,  $g_D = 10^{-7}$ ,  $\epsilon = 3.8 \times 10^{-7}$ ,  $\delta = 0$ ,  $\sin \beta = 0$ ,  $T_{RH} = 1$  TeV,  $\xi_0 = 0.01$

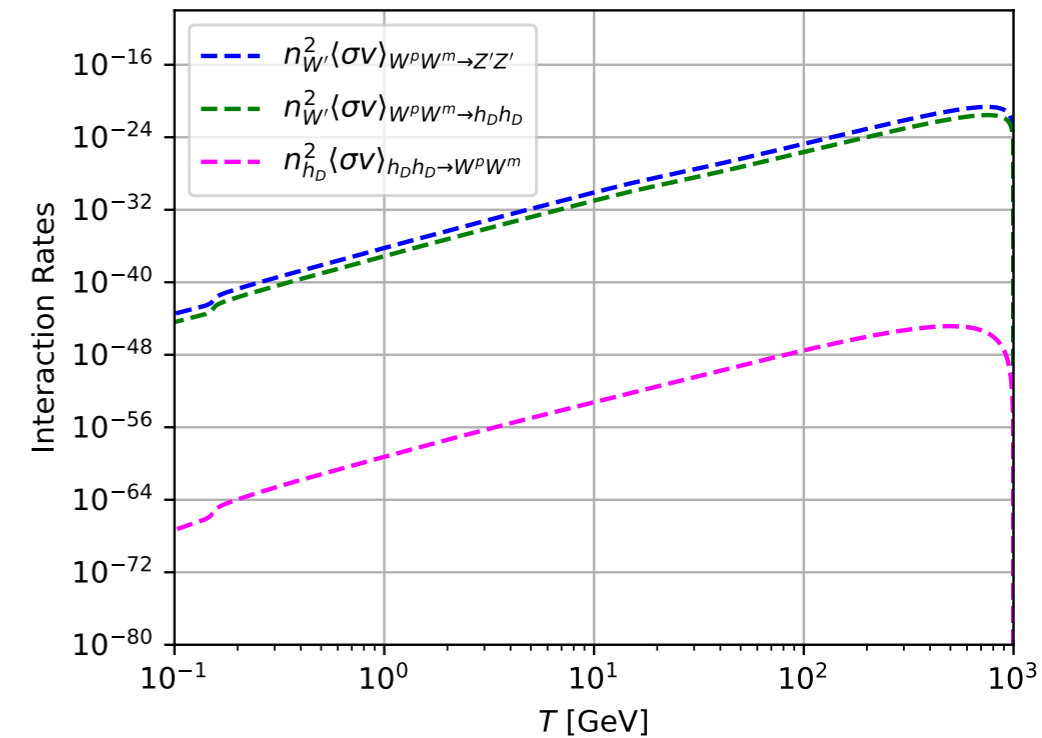
❖ Relic of **dark photon** and **dark Higgs** are subdominant as suppressed by tiny  $g_D$



❖ Dominated by milli-charged annihilation process  $f\bar{f} \rightarrow W^p W^m$



❖ **Z** and **plasmon** decays sub-dominated





# DM relic abundance vs. $N_{\text{eff}}$ vs. Reheating Temp.

BM :  $m_{W'} = 0.01 \text{ GeV}$ ,  $m_{h_D} = m_{W'}/3$ ,  $g_D = 10^{-7}$ ,  $\epsilon = 3.8 \times 10^{-7}$ ,  $\delta = 0$ ,  $\sin \beta = 0$ ,  $T_{\text{RH}} = 1\text{TeV}$

❖ Light new particles contribute to the effective neutrino number  $N_{\text{eff}}$

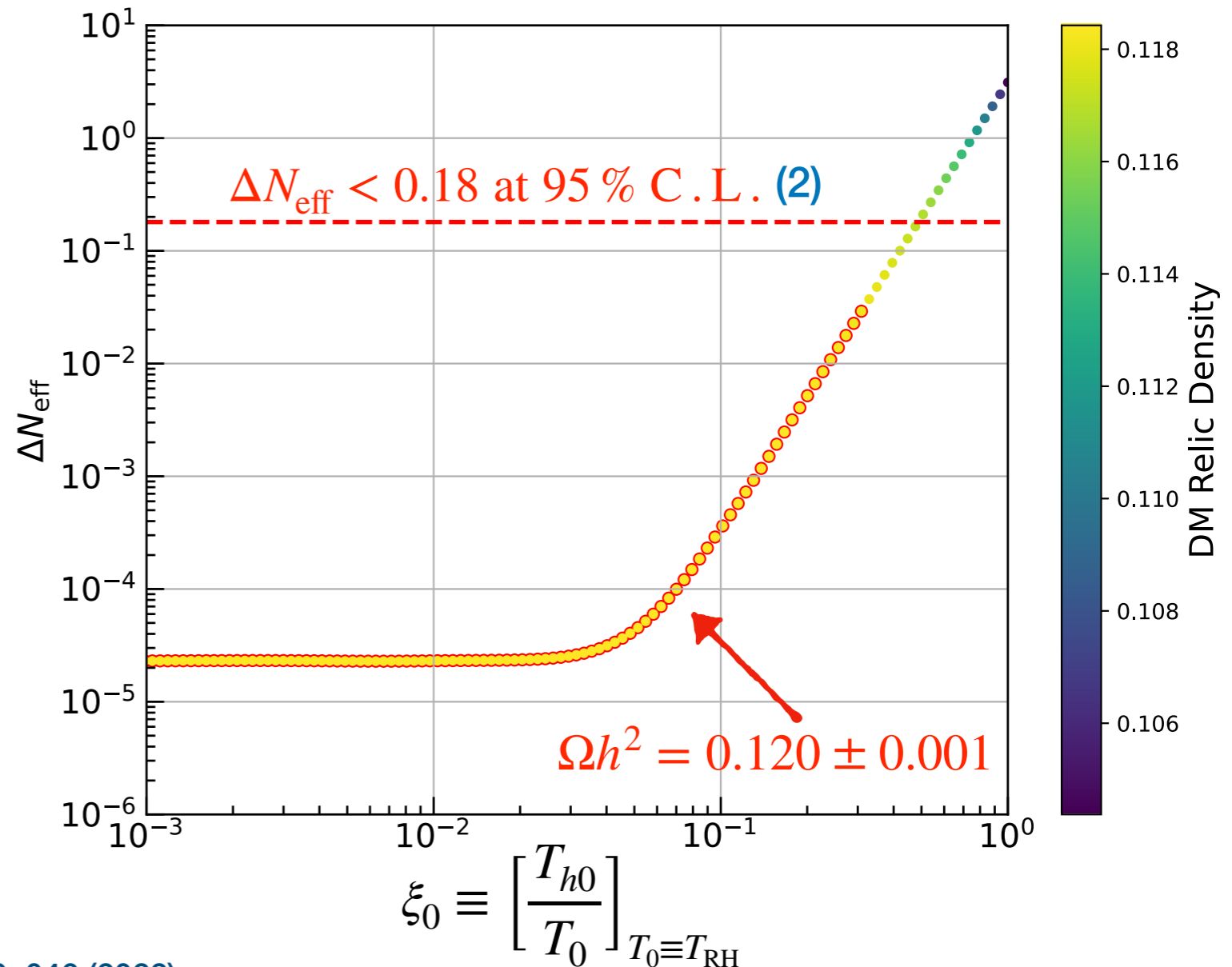
❖ The reheating temperature is unknown -> affects initial condition.

❖ Initial condition of temperature ratio between two sectors affects both the DM relic abundance and  $N_{\text{eff}}$

❖ Larger  $\xi_0$  enhances  $\Delta N_{\text{eff}}$  while suppressed DM relic abundance

❖  $\xi_0 \gtrsim 0.5$  is excluded by BBN and CMB

$$\Delta N_{\text{eff}}(T, \xi) \Big|_{\text{BBN}} = \frac{4}{7} g_{\text{eff}}^h(T) \left( \frac{11}{4} \right)^{4/3} \xi(T)^4 \Big|_{\text{BBN}} \quad (1)$$



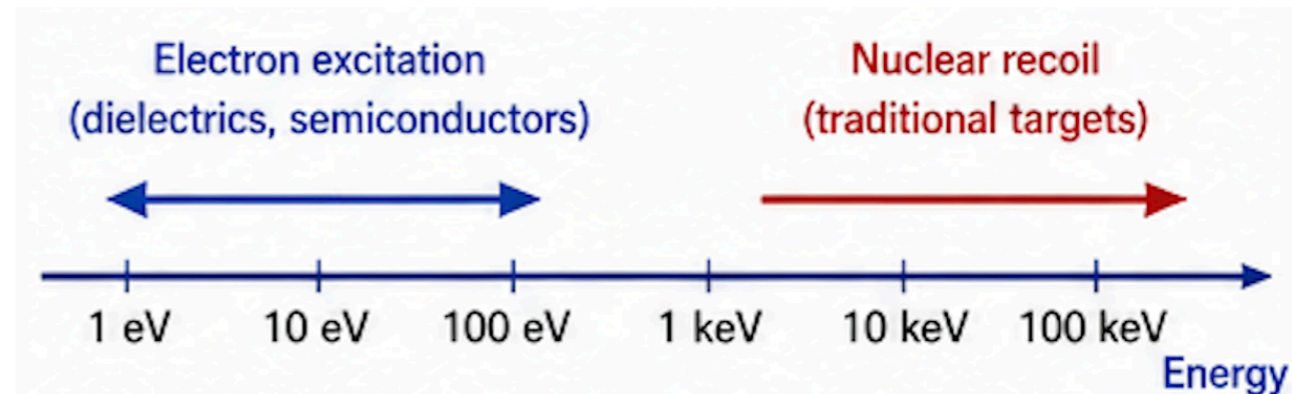
(1) J. Li and P. Nath, Phys.Rev.D 108 (2023) 11, 115008; +++

(2) T.-H. Yeh, J. Shelton, K. A. Olive, and B. D. Fields, JCAP 10, 046 (2022)



# Search for sub-GeV DM

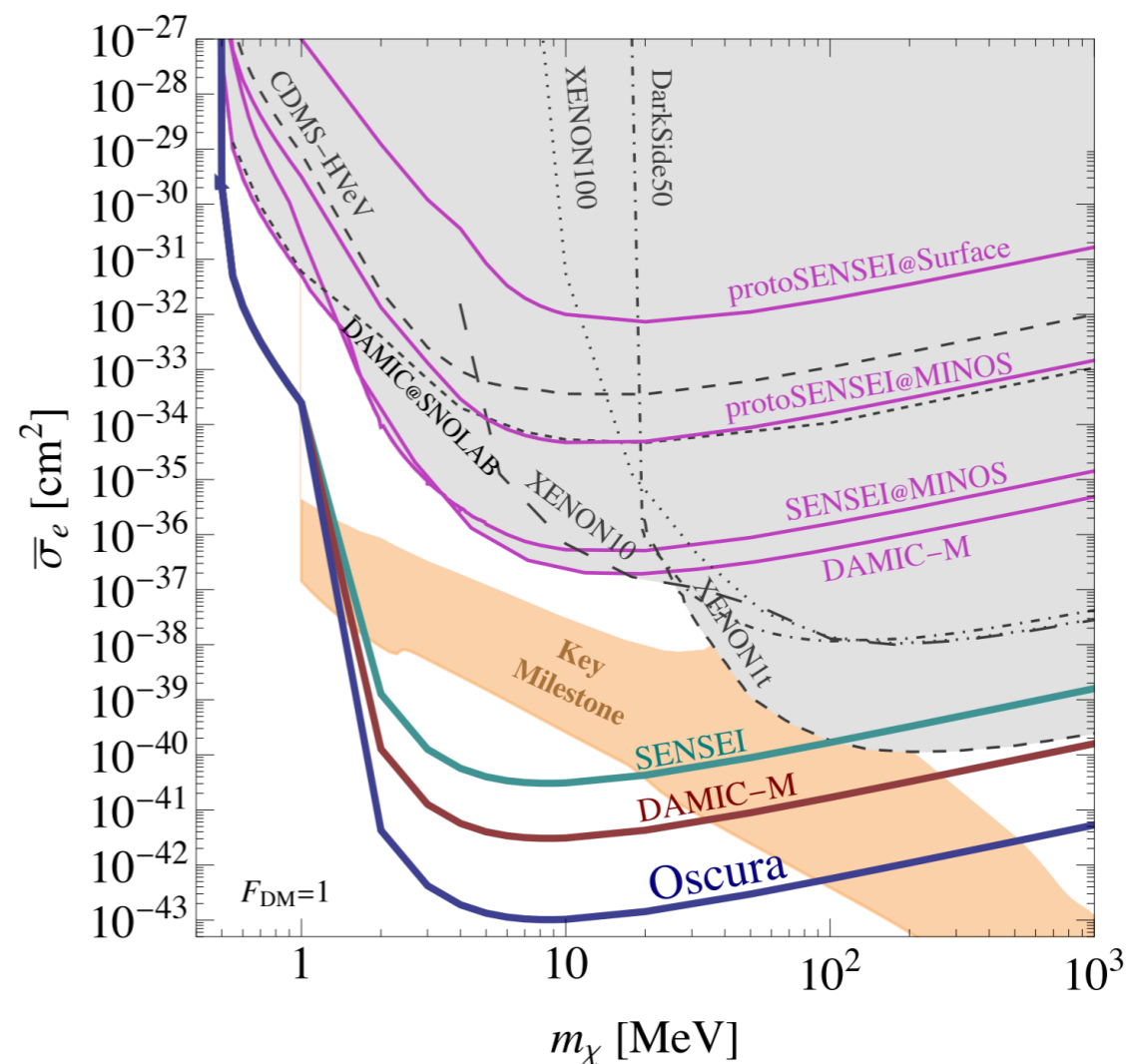
◆ **Sub-GeV DM gives too little energy to nuclei but can **efficiently scatters of electrons****



◆ **Silicon charge-coupled devices w/ Skipper amplification (**Oscura, SENSEI, DAMIC-M**)**

- ❖ Skipper amplifier makes repetitive, non-destructive measurement of the pixel charge, reducing noise to sub-electron levels -> **Ultra low noise**
- ❖ **Sensitive to tiny ionization**
- ❖ **Low threshold enables low-mass searches (1-1000 MeV DM)**

◆ **Other proposals are also investigating alternative target materials, such as superconductors and polar crystals.**



arXiv:2304.04401

- ❖ **Electron recoils** from the process  $W' + e^- \rightarrow W' + e^-$  for **sub-GeV DM**

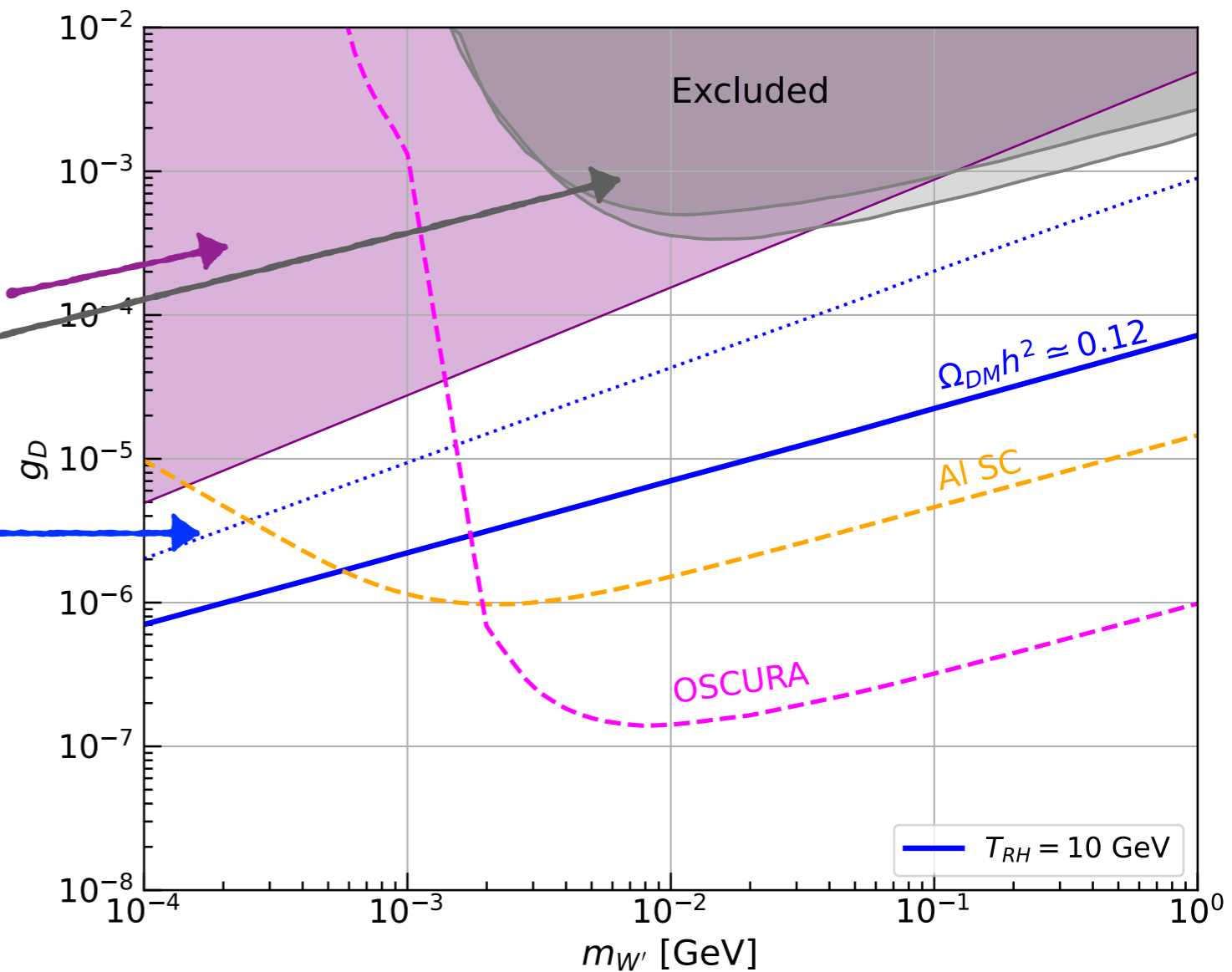
- ❖ Dominated by photon exchange, while  $Z$  and scalar mediated contributions being sub-leading

- ❖ Shaded regions are excluded by **SIDM from NGC720 galaxy ellipticity** and by **DMDD from SENS, DAMIC ...**

- ❖ DM abundance can be depleted for large  $g_D$  due to  $W^p W^m \rightarrow Z' Z'$  and to other DS

- ❖ Probed by projected sensitivities from **OSCURA (1)** and **ALSC (2)** (Aluminum based superconducting detectors)

$BM : m_{h_D} = m_{W'}/3, \epsilon = 0.5 \times 10^{-7}, \delta = 0, \xi_0 = 0.01$

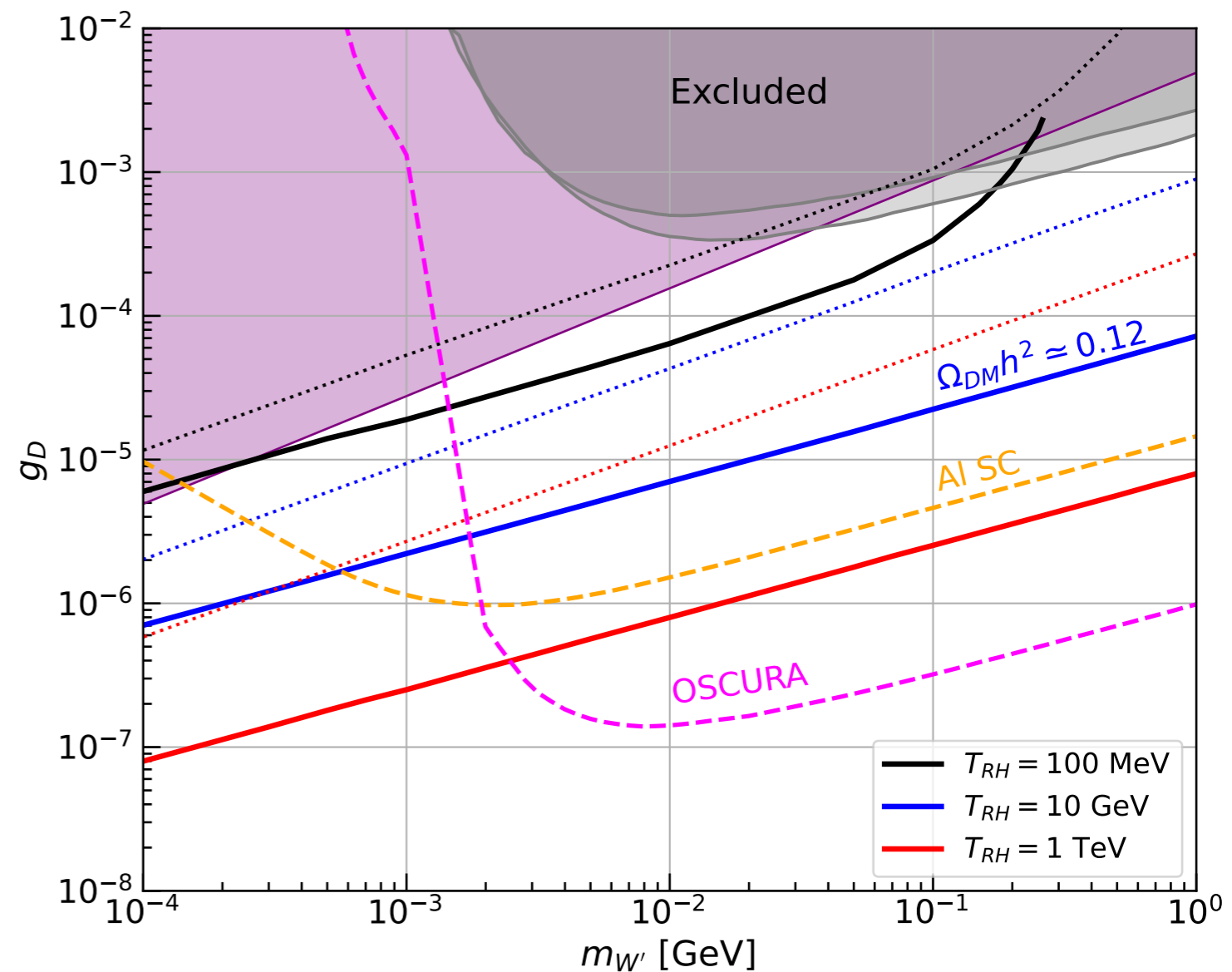


(1) B. A. Cervantes-Vergara et al. (Oscura), JINST 18, P08016 (2023), arXiv:2304.04401

(2) Y. Hochberg et al. Phys. Rev. Lett. 127, 151802 (2021), arXiv:2101.08263

- ❖ **Electron recoils** from the process  $W' + e^- \rightarrow W' + e^-$  for **sub-GeV DM**
- ❖ Dominated by photon exchange, while  $Z$  and scalar mediated contributions being sub-leading
- ❖ Shaded regions are excluded by **SIDM from NGC720 galaxy ellipticity** and by **DMDD from SENS, DAMIC ...**
- ❖ DM abundance can be depleted for large  $g_D$  due to  $W^p W^m \rightarrow Z' Z'$  and to other DS
- ❖ Probed by projected sensitivities from **OSCURA (1)** and **ALSC (2)** (Aluminum based superconducting detectors)
- ❖ **Relic density is sensitive to low  $T_{RH}$**
- ❖ **SIDM and DMDD can put a lower bound on  $T_{RH}$**

$BM : m_{h_D} = m_{W'}/3, \epsilon = 0.5 \times 10^{-7}, \delta = 0, \xi_0 = 0.01$



(1) B. A. Cervantes-Vergara et al. (Oscura), JINST 18, P08016 (2023), arXiv:2304.04401

(2) Y. Hochberg et al. Phys. Rev. Lett. 127, 151802 (2021), arXiv:2101.08263



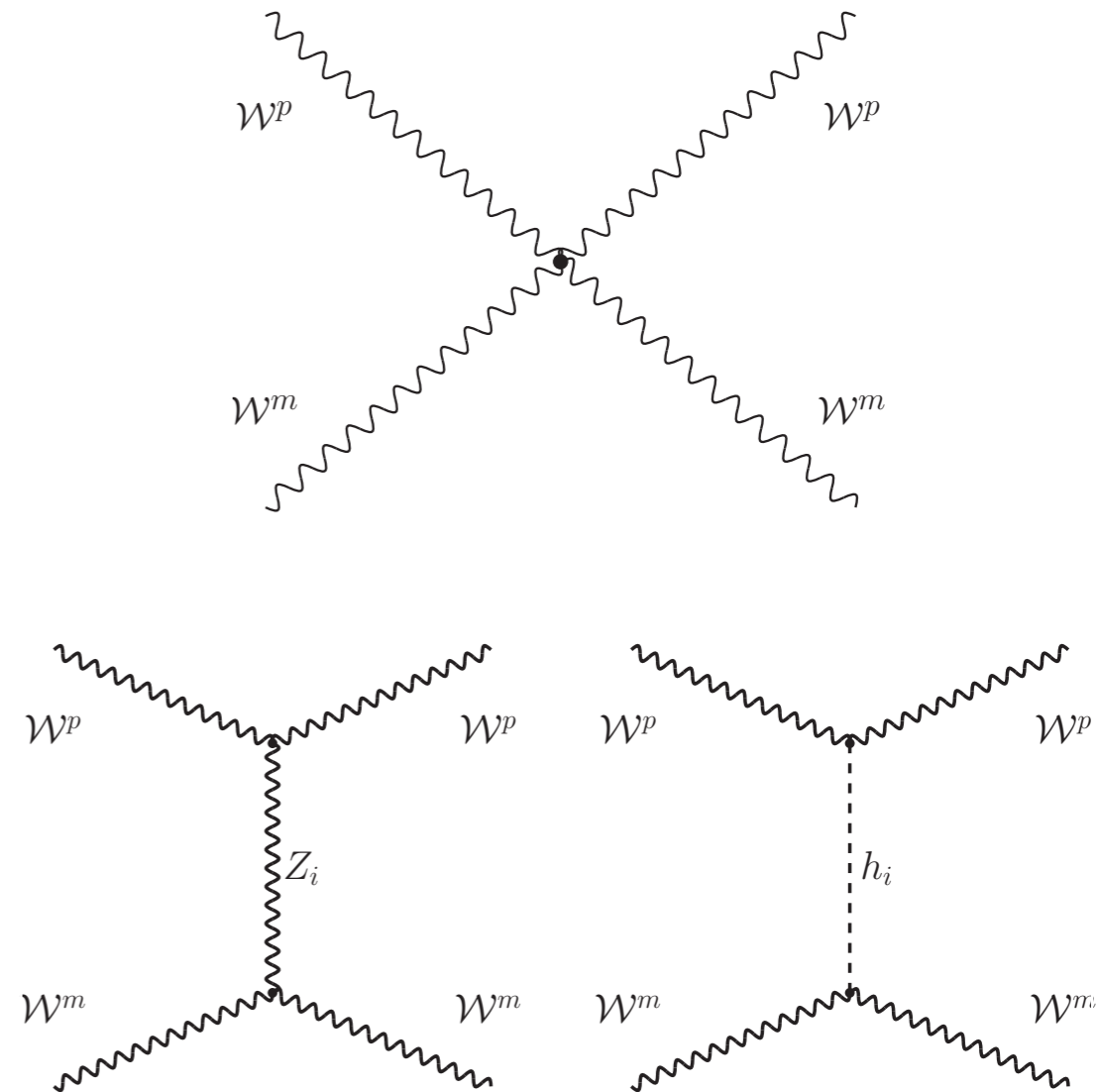
- ◆ **Hidden sector** provides a well-motivated framework for dark matter, naturally featuring feeble interactions with SM particles.
- ◆ The **portal particles** may exhibit long lifetimes, making them promising targets for searches at future **long-lived particle** (LLP) detectors.
- ◆ We propose a simple yet realistic model of **two-temperature universe** based on  $G_{\text{SM}} \otimes SU(2)_D + \Sigma_D$  and **Abelian–Non-Abelian** kinetic mixing.
- ◆ **Non-Abelian gauge bosons** becomes a viable **millicharged freeze-in DM** candidate.
- ◆ **Future low-threshold direct-detection** experiments can probe this **sub-GeV DM** via electron scattering.
- ◆ The two-temperature Universe may also generate observable **gravitational-wave signals** from a strongly first-order phase transition.

Thank You

- ◆ Ellipticity profile of the galaxy sets stringent bound on dark sector **self-interactions** (SIDM)
- ◆ Limits from NGC720 galaxy (1) by the evolution of the velocity anisotropy due to energy transfer:

$$m_{\text{DM}} \left( \frac{0.01}{\alpha_D} \right)^{2/3} \gtrsim 300 \text{ GeV}$$

- ◆ SIDM helps to solve **small scale problems** (core-cusp, too big to fail, missing satellites) (2)



(1) Agrawal, Cyr-Racine, Randall, and Scholtz (JCAP 1705(05), 022 (2017))

(2) S. Tulin and H. B. Yu, Phys. Rept. 730, 1-57 (2018); VQT, Nguyen, and Yuan, JCAP 05 (2024) 015; +++

$$J_h \simeq \sum_f \left\{ n_f^2 \left[ 2J_{f\bar{f} \rightarrow W^p W^m}(T) + J_{f\bar{f} \rightarrow h_D}(T) \right] \right. \\ \left. + 2n_Z J_{Z \rightarrow W^p W^m}(T) + 2n_h J_{h \rightarrow W^p W^m}(T) \right. \\ \left. + 2n_{\gamma^*} J_{\gamma^* \rightarrow W^p W^m}(T) - n_{h_D} J_{h_D \rightarrow f\bar{f}}(T_h) \right\} ,$$



$$\begin{aligned}
 \mathcal{R}_{W'}(T, T_h) = & \sum_{f \in \text{SM}} \left[ n_f^2 \langle \sigma v \rangle_{f\bar{f} \rightarrow W' P W^m}(T) \right] + n_Z \langle \Gamma \rangle_{Z \rightarrow W' P W^m}(T) + n_h \langle \Gamma \rangle_{h \rightarrow W' P W^m}(T) \\
 & + n_{\gamma^*} \langle \Gamma \rangle_{\gamma^* \rightarrow W' P W^m}(T) + n_{h_D} \langle \Gamma \rangle_{h_D \rightarrow W' P W^m}(T_h) \\
 & + n_{h_D}^2 \langle \sigma v \rangle_{h_D h_D \rightarrow W' P W^m}(T_h) - n_{W'}^2 \left[ \langle \sigma v \rangle_{W' P W^m \rightarrow h_D}(T_h) \right. \\
 & \left. + \langle \sigma v \rangle_{W' P W^m \rightarrow Z' Z'}(T_h) + \langle \sigma v \rangle_{W' P W^m \rightarrow h_D h_D}(T_h) \right],
 \end{aligned}$$

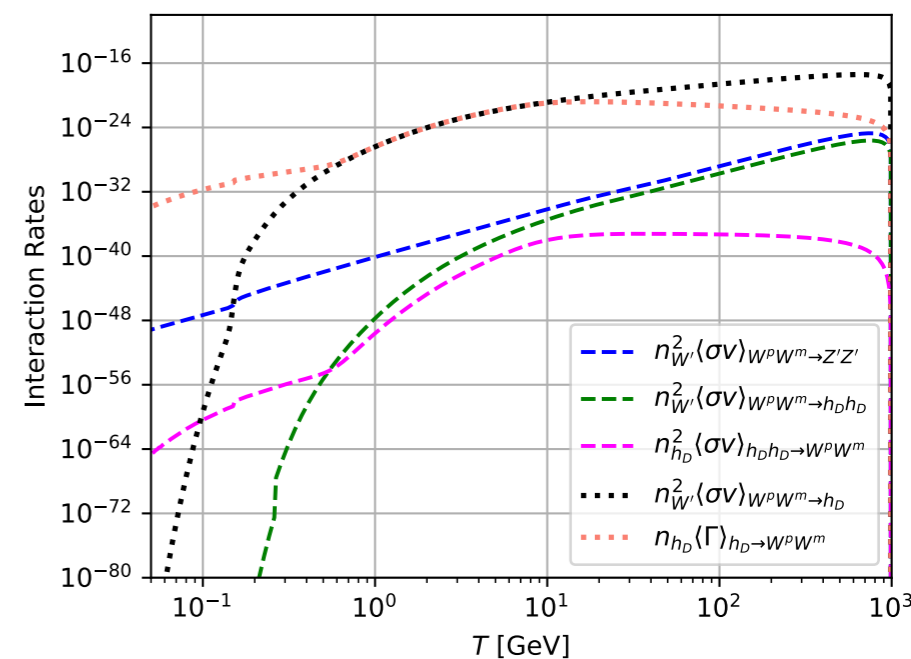
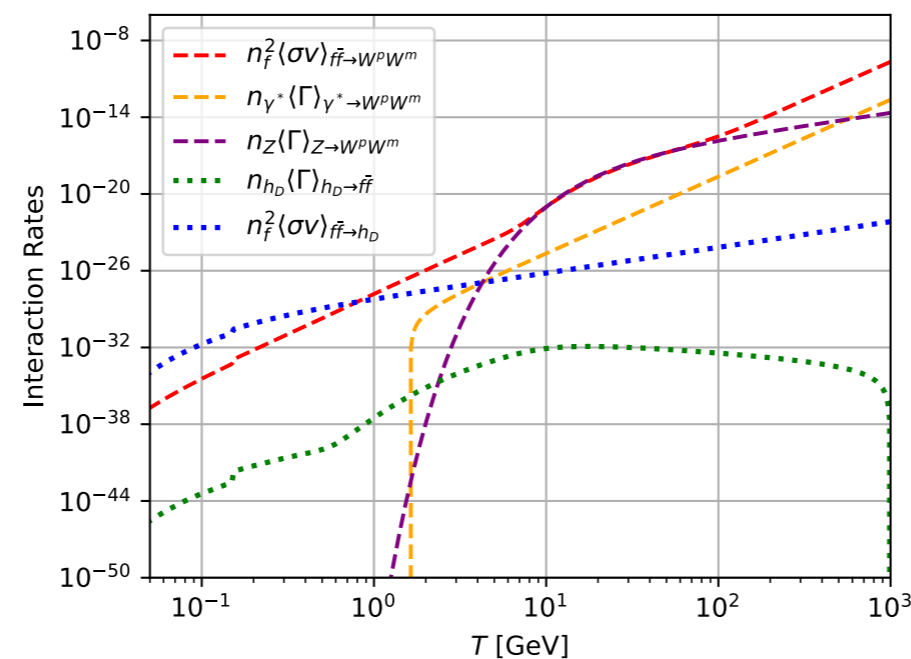
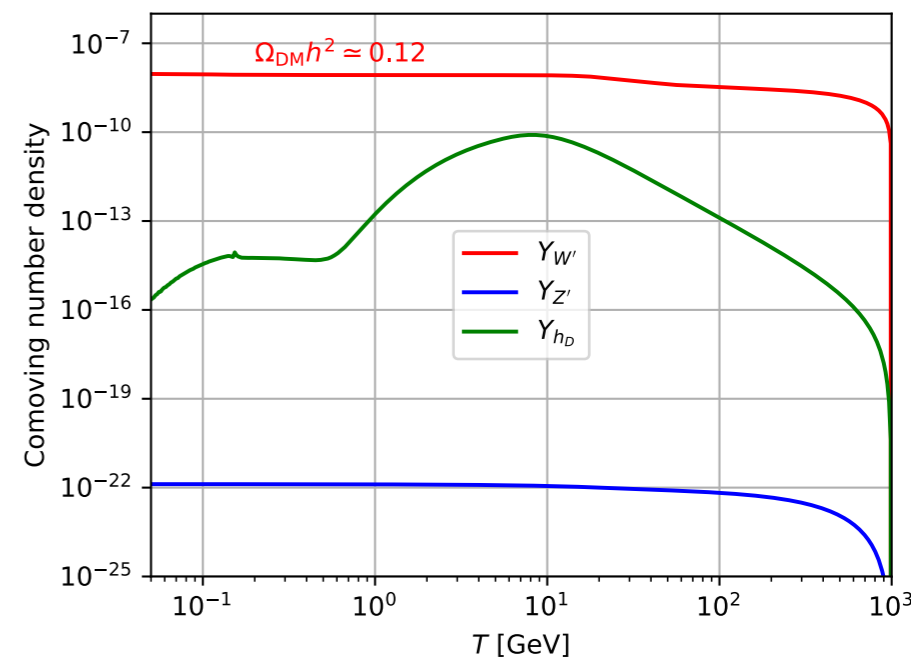
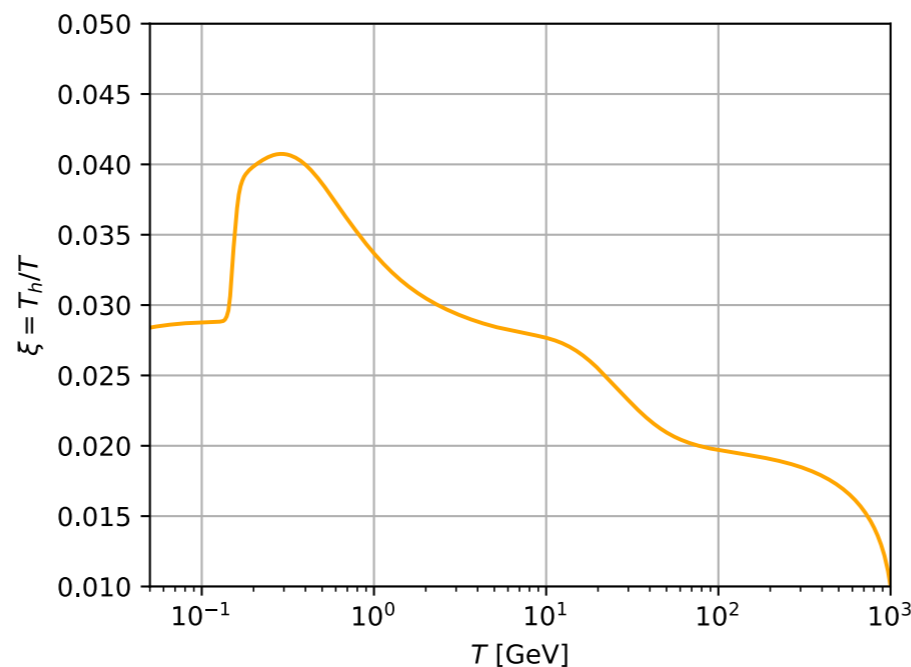
$$\mathcal{R}_{Z'}(T, T_h) = n_{W'}^2 \langle \sigma v \rangle_{W' P W^m \rightarrow Z' Z'}(T_h),$$

$$\begin{aligned}
 \mathcal{R}_{h_D}(T, T_h) = & \sum_{f \in \text{SM}} \left[ n_f^2 \langle \sigma v \rangle_{f\bar{f} \rightarrow h_D}(T) \right] + n_{W'}^2 \left[ \langle \sigma v \rangle_{W' P W^m \rightarrow h_D h_D}(T_h) \right. \\
 & \left. + \langle \sigma v \rangle_{W' P W^m \rightarrow h_D}(T_h) \right] - n_{h_D}^2 \langle \sigma v \rangle_{h_D h_D \rightarrow W' P W^m}(T_h) \\
 & - n_{h_D} \left[ \langle \Gamma \rangle_{h_D \rightarrow W' P W^m}(T_h) + \sum_{f \in \text{SM}} \langle \Gamma \rangle_{h_D \rightarrow f\bar{f}}(T_h) \right].
 \end{aligned}$$

$$m_{W'} = 0.1 \text{ GeV}, m_{h_D} = 0.4 \text{ GeV}, g_D = 10^{-7}, \epsilon = 1.2 \times 10^{-6}, \delta = 0, \sin \beta = 10^{-9}$$

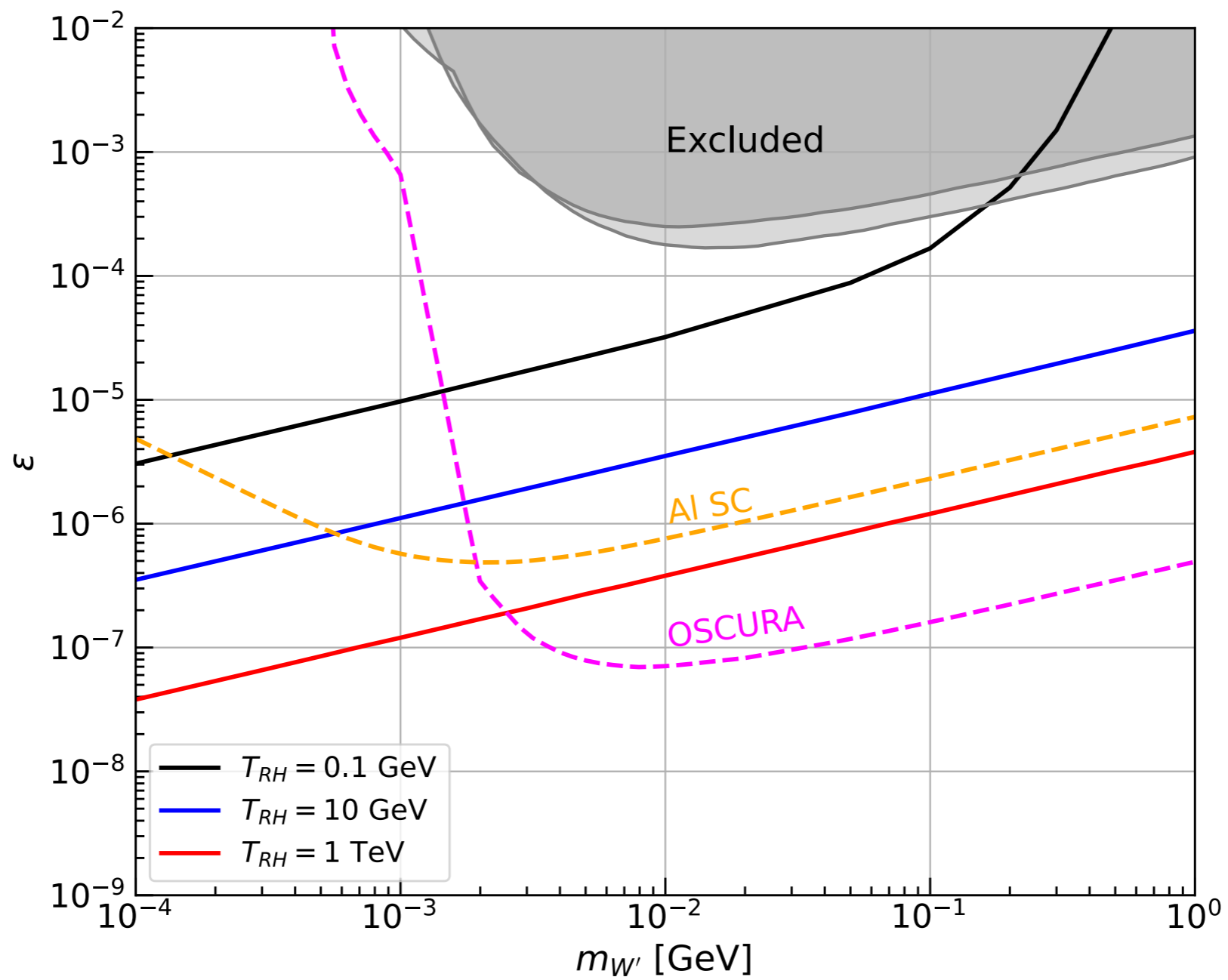
❖ Presence of **non-zero Higgs dark scalar mixing** opens an additional portal interaction between the dark sector and the SM.

❖ Richer features in the evolution of  $\xi$  and the enhancement of dark Higgs boson yield



# Backup: $(\epsilon, m_{W'})$ plane

BM :  $m_{h_D} = m_{W'}/3$ ,  $g_D = 10^{-7}$ ,  $\delta = 0$ ,  $T_{RH} = 1\text{TeV}$ ,  $\xi_0 = 0.01$



◆ The process of  $W^+ W^-$  to two physical photons

$$\begin{aligned}\sum_{\text{pol.}} |M|_{W^+W^- \rightarrow 2 \text{ photons}}^2 &= \frac{1}{2} \left( \sum_{\text{pol.}} |M|_{W^+W^- \rightarrow \gamma\gamma}^2 + \sum_{\text{pol.}} |M|_{W^+W^- \rightarrow Z'Z'}^2 \right) + \sum_{\text{pol.}} |M|_{W^+W^- \rightarrow \gamma Z'}^2 \\ &= g^4 (\mathcal{O}_{21}^4 + \mathcal{O}_{23}^4 + 2\mathcal{O}_{21}^2 \mathcal{O}_{23}^2) \times F \\ &= e^4 \times F\end{aligned}$$

- ❖ Where  $\mathcal{O}_{ij}$  is the neutral gauge bosons matrix rotation and  $F$  is the common invariant function of Mandelstam variables
- ❖ It is independence on the rotation angle  $\alpha$



Monojet at ATLAS

Invisible Z decay

